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Ministry of Education &
Technical Education
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Book Affairs

Mathematics

Fifth Primary

5

Student's Book
Second Term

Revised by

Mr/ Samir Mohamed Sedawy



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غير مصرح بتداول هذا الكتاب خارج
وزارة التربية والتعليم والتعليم الفني

Authors

Mr. Omar Fouad Gaballa

Prof.Dr. Afaf Abo-ElFoutoh Salah **Dr.** Essam Wasfi Roupheail

Mr. Mahmoud Yasser Al-khatieb **Mr.** Serafiem Elias ESkander

Revised by

Mr. Samir Mohamed Sedawy

Mr. Hussein Mahmoud Hussein

Counsellor of Mathematics

M.O.E

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بسم الله الرحمن الرحيم

Dear students:

It is extremely great pleasure to introduce the mathematics book for fifth primary. We have been specially cautious to make learning mathematics enjoyable and useful since it has many practical applications in real life as well as in the other subjects. This gives you a chance to be aware of the importance of learning mathematics, to determine its value and to appreciate the mathematicians roles.

This book sheds new lights on the activities as a basic objective. Additionally, we have tried to introduce the subject simply and excitingly to help attaining mathematical knowledge as well as gaining the patterns of positive thinking skills which pave your way to creativity.

This book is divided into units, each unit contains lessons. Colors and pictures are effectively used to illustrate some mathematical concepts and the properties of figures. Lingual level of previous study has also been taken into consideration.

Our great interest here is to help you get the information by your self in order to develop your self-Learning skills.

Calculators and computer sets are used when there's a need for. Exercises, practices, general exams, activities, unit test, general tests, and final term tests attached with model answers have been included to help you review the curriculum completely.

Eventually, we hope getting on the right track for the benefits of our students as well as for our dearest Egypt hoping bright future to our dearest students.

Authors



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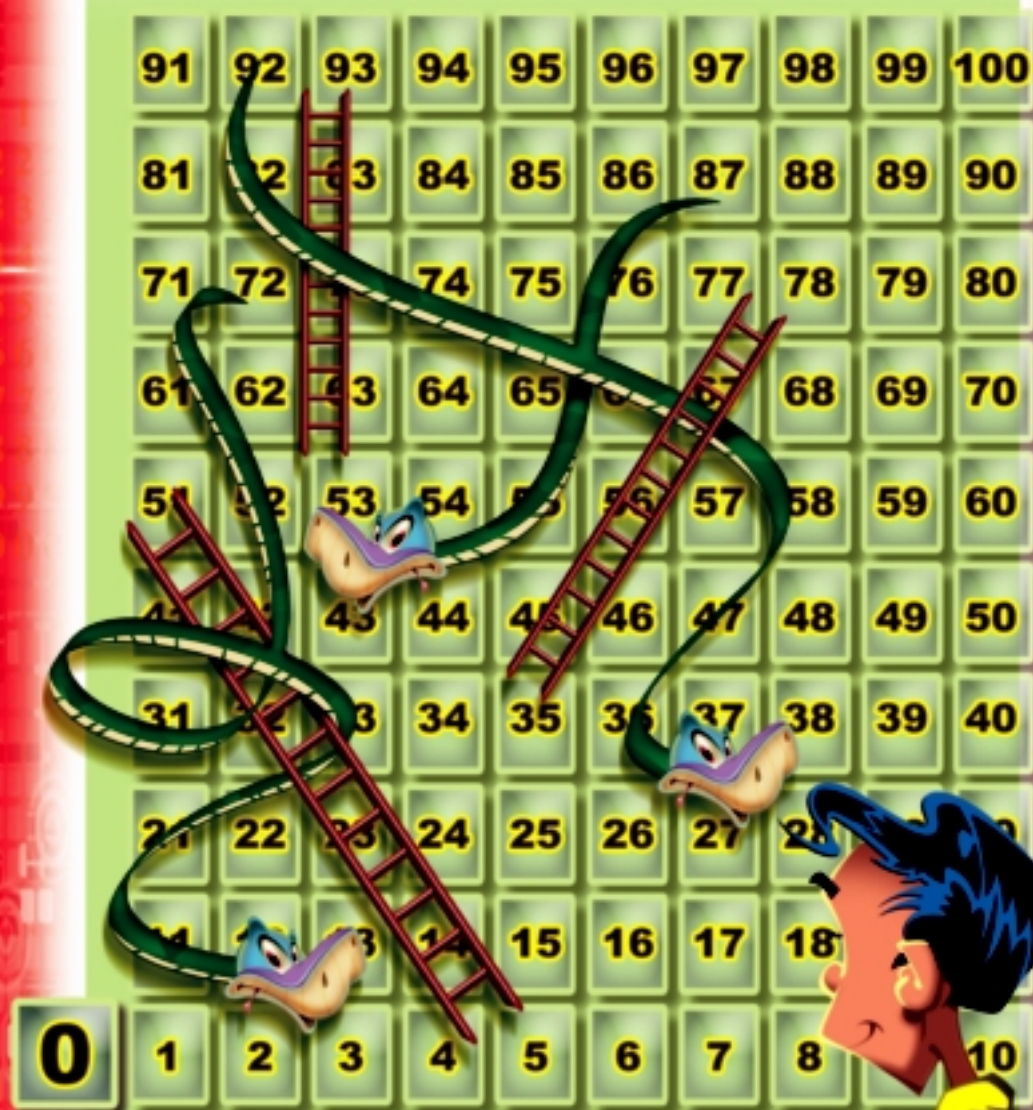
List of Symbols

C	Set of counting Numbers	\leq	Less than or equal to
E	Set of Even numbers	$=$	Equal to
O	Set of Odd numbers	\neq	Not Equal to
P	Set of prime numbers		Open curve
\emptyset or $\{ \}$	Null set or empty set		Closed Curve
\in	Belonging		Circle
\notin	Not belonging	r	radius
\subset	Inclusion	π	Approximate ratio
$\not\subset$	Not inclusion	\overline{AB}	Line segment A B
\cup	Union	\overrightarrow{AB}	Ray A B
\cap	Intersection	$\longleftrightarrow AB$	Straight line A B
U	Universal set	\angle	Angle
X'	Complement set	$m (\angle B)$	Measure angle (B), $m (\angle B)$
X-Y	X difference Y	$P (E)$	Probability of event E $P (E)$
N	Set of natural numbers	\equiv	Congruent
$>$	greater than	\triangle	Triangle
\geq	greater than or equal to	(x, y)	Ordered pair X, y (x, y)
$<$	Less than		

Unit one

Natural Numbers

1



Set of Natural Numbers



Think and Discuss

* You will learn *

- ☺ Set of natural numbers



Key Terms

- ▶ Set of natural numbers (N)
- ▶ Infinite set

If you want to count your classmates, with which number will you start?

Counting starts with 1 then 2, 3 and so on.

What is the meaning of your last number?

Set of Counting Numbers

The set of counting numbers = $\{1, 2, 3, 4, \dots\}$ and it is an infinite set. Adding the element "0" to this set produces a new set denoted by N and called set of **natural numbers**, where : $N = \{0, 1, 2, 3, 4, \dots\}$

$$N = \{0, 1, 2, 3, 4, \dots\}$$

It is an infinite set.

Example

Complete using an appropriate notation of \in , \notin , \subset and $\not\subset$ to get a true statement .

A zero N

B 2222 N

C 22.22 N

D $\{2222\}$ N

E $\{2, 0.2\}$ N

Solution:

A \in

B \in

C \notin

D \subset

E $\not\subset$



Write down two sets, one of them is a subset of N and the other one is not a subset of N .

Exercises

- 1 Complete using an appropriate notation of \in , \notin , \subset and $\not\subset$ to get a true statement .

A $2 \dots\dots N$

B $\{2\} \dots\dots N$

C $\frac{3}{4} \dots\dots N$

D $0.7 \dots\dots N$

E $\{55\} \dots\dots N$

F $\{2, 4, 6\} \dots\dots N$

G $\{1, 3\} \cap \{2, 4\} \dots\dots N$

H zero $\dots\dots N$

- 2 Complete :

A The smallest natural number is

B The smallest counting number is

C The set of natural numbers less than 5 is.....

D Natural numbers \cap Counting numbers ($N \cap C$) =

- 3 Match (✓) with true statements and (✗) with false statements.

A $7.2 \in N$ ()

B $\{0\} \subset N$ ()

C $\{0\} \cup \{1, 2, 3\} = N$ ()

D $\{0, 1, 2\} \cap \{0, 5, 10\} = \emptyset$ ()

E The greatest natural number is milliard. ()

F The set of natural numbers is infinite. ()

Some Subsets of N



Think and Discuss

* You will learn *

- ☺ Some subsets of N
- ☺ Set of even numbers
- ☺ Set of odd numbers
- ☺ Set of prime numbers.



Key Terms

- ▶ Subset.
- ▶ Set of even numbers (E).
- ▶ Set of odd numbers (O)
- ▶ Set of prime numbers (P)

You have learned that the set of natural numbers

$$N = \{0, 1, 2, 3, 4, \dots\}$$

The set of natural numbers N can be represented on the number line as follows:

Set of natural numbers (N)

Set of even numbers (E)

Set of odd numbers (O)

Set of prime numbers (P)

From the references above you find that :

$$\text{Set of even numbers (E)} = \{0, 2, 4, 6, \dots\}$$

$$\text{Set of odd numbers (O)} = \{1, 3, 5, \dots\}$$

$$\text{Set of prime numbers (P)} = \{2, 3, 5, 7, \dots\}$$

Find :

$E \cup O$

$E \cap O$

$N \cap P$

$E \cap P$

What do you observe?



Draw a Venn diagram to represent the sets : N, O and E .

Example

Complete the following to get a true sentence:

- A The set of natural numbers less than 5 is
 B $N \cup O = \dots\dots\dots$ where O is the set of odd numbers.
 C $\{15, 6, 0, 4\} \cap N = \dots\dots\dots$
 D $E \cap P = \dots\dots\dots$ where E is the set of even numbers and P the set of prime numbers.
 E $E - O = \dots\dots\dots$

Solution

- A $\{0, 1, 2, 3, 4\}$ B N C $\{15, 6, 0, 4\}$
 D $\{2\}$ E E

Exercises

1 Match (✓) with true statements and (✗) with false ones.

- A Weight of anything in kgs $\in N$. ()
 B Your cellphone number $\in N$. ()
 C Number of pages of a book $\in N$. ()
 D The smallest prime number is 1. ()

2 Complete :

- A The set of natural numbers (N) - The set of even numbers (E) =
 B The set of even numbers (E) \cap The set of odd numbers (O) =
 C The set of even numbers (E) $\cap \{0, 1, 2\} = \dots\dots\dots$
 D $\{0, 2\} \cap$ The set of prime numbers (p) =

3 Use venn-diagram to express the sets :

- The set of natural numbers (N) ,
 The set of even numbers (E) ,
 The set of odd numbers (O) ,

Ordering and Comparing Natural Numbers

* You will learn *

- ☺ To represent natural numbers N on the number line.
- ☺ To order and compare natural numbers.



Key Terms

- ▶ Ordering numbers
- ▶ Comparing numbers

I: Representing natural numbers (N) on the number line.



Let's work together

Classmates have to work in pairs:

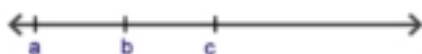
- 1 Draw a straight line.



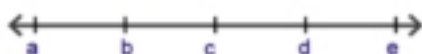
- 2 Choose two points a and b on the line.



- 3 Determine the point c on the line, where $ab = bc$



- 4 Determine the points d, e, \dots on the line, where $ab = bc = cd = de$.



- 5 Place the numbers $0, 1, 2, 3, 4, \dots$ to correspond the points a, b, c, d, e, \dots



Remark

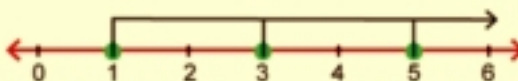
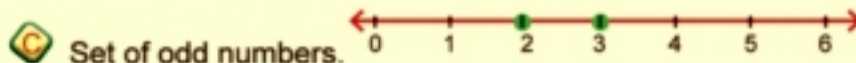
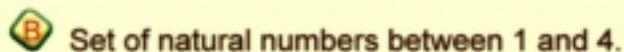
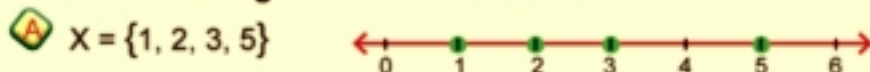
The natural number 3 is placed directly to the right of the number 2 and directly to the left of the number 4.

Complete:

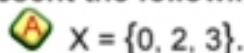
The number 2 is placed directly to the right of the numberand directly to the left of the number

Examples

Represent the following sets on the number line :

**Practice**

Represent the following sets on the number line :



Represent on the number line $X \cup Y$, where: $X = \{1, 2, 3, 5\}$, $Y = \{5, 6, 7\}$
then find $X \cap Y$

II: Ordering and comparing natural numbers.

Let's work together



Work with your classmate.

- 1** Draw a number line and place the numbers which represent the set of natural numbers on it.

- 2** Complete:

The number 2 is placed directly to the right of the number, Therefore $2 > \dots$,
While number 2 is placed directly to the left of the number, Therefore $2 < \dots$

The number 4 is placed directly to the right of the number and to the left of the number, Therefore $4 > \dots$, $4 < \dots$

In general:

For any two natural numbers represented on the number line a and b :

- ☹ If the point that represents the number b is



placed to the right of the point that represents the number a , then $b > a$

- ☹ If the point that represents the number a is placed to the left of the point that represents the number b , then $a < b$

**Practice**

- 1 If the following natural numbers a, b, c, d and e are represented on a number line as shown on the figure below:



I : Complete using $>$ or $<$ and justify your answer:

- A a ☐ b because a is placed to the right of b .
 B b ☐ e because b is placed to the left of e .
 C c ☐ e because.....
 D e ☐ b because.....
 E a ☐ d because.....
 F c ☐ d because

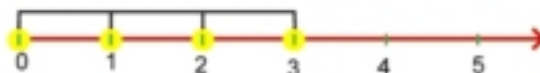
II : The ascending order is

- 2 Represent on a number line.

- A The set of natural numbers between 1 and 4



- B The set of natural numbers less than 4



- C The set of natural numbers greater than or equal to 4, and written as $X \geq 4, X \in \mathbb{N}$



Exercises

- 1 Write the following sets using the listing method and represent them on a number line:

$$X = \{a : a \in \mathbb{N}, \text{ where } a \text{ is between } 0, 4\}$$

$$Y = \{a : a \in \mathbb{N}, a \geq 3\}$$

$$Z = \{a : a \in \mathbb{N}, a < 6\}$$

$$M = \{a : a \in \mathbb{N}, 2 \leq a \leq 5\}$$

- 2 Write down the represented set on the following number lines:



- 3 Find the ascending order of 5, 0, 2, 4, 1 and represent them on a number line.

- 4 Represent the following on a number line:

- A The set of prime factors of 30.
- B The set of prime numbers less than 25.

Operations on Natural Numbers



Think and Discuss

* You will learn *

- ☺ Operations on natural numbers
- ☺ Addition operation in N
- ☺ Subtraction operation in N
- ☺ Multiplication operation in N
- ☺ Division operation in N



Key Terms

- ▶ Adding two natural numbers.
- ▶ Closure and commutative properties
- ▶ Associative property
- ▶ Additive neutral element
- ▶ Distribution property
- ▶ Subtraction in N
- ▶ Multiplicative neutral element

I: Addition Operation in N

The teacher of Mohamed and Hoda asked them to think about a way to add two numbers such as 2 and 4 on the number line:

Mohamed said

I will start at 0 moving two units to the right, then 4 units in the same direction, then I reach the number 6. **Thus, $2 + 4 = 6$**

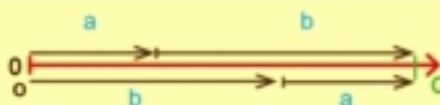


Hoda said

I will start at 0 moving first 4 units to the right, then two units in the same direction. Then I will reach the number 6. **Thus, $4 + 2 = 6$**



i.e: $2 + 4 = 4 + 2 = 6$



In general: for any two natural numbers a and b : $a + b = b + a$

Commutative property of adding in N .

Remarks



For any two natural numbers a and b :

$$a + b = c, \text{ where } c \in \mathbb{N} \quad \text{i.e. } 2 + 3 = 5, 5 \in \mathbb{N}$$

Closure property of adding in \mathbb{N} .



$$(2 + 3) + 7 = 5 + \dots = 12, \quad 2 + (3 + 7) = \dots + 10 = 12$$

$$\text{i.e. } (2 + 3) + 7 = 2 + (3 + 7) = 2 + 3 + 7 = 12$$

For any three natural numbers a , b and c :

$$(a + b) + c = a + (b + c) = a + b + c$$

Associative property of adding in \mathbb{N} .



$$6 + 0 = 6 \quad \text{also } 0 + 6 = 6$$

$$\text{i.e. } 6 + 0 = 0 + 6 = 6$$

For any natural number a : $a + 0 = 0 + a = a$

Therefore: zero is the additive neutral element of adding in \mathbb{N} .

Practice

Complete to get a true sentence:



$$213 + 57 = 57 + \dots$$

..... Property



$$28 + (72 + 59) = (28 + \dots) + 59 = \dots + 59 = \dots$$

..... Property



$$0 + 4365 = \dots$$

..... Property

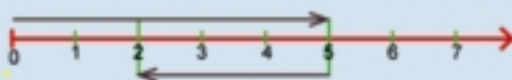
$(999 + 487) + 1 = 999 + (\dots + 1) \dots \text{Property}$
 $= 999 + (1 + \dots) \dots \text{Property}$
 $= (999+1) + \dots \dots \text{Property}$
 $= \dots + \dots$
 $= \dots$

II : Subtraction in N

Subtract if possible:

A $5 - 3$

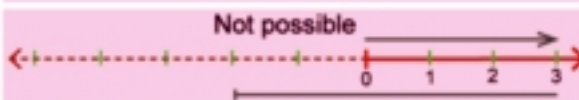
To calculate $5 - 3$



$5 - 3 = 2$ Possible

B $3 - 5$

To calculate $3 - 5$



$3 - 5$ Not possible

Remark

- ⊗ Subtraction operation is sometimes not possible in N.
- ⊗ For any two natural numbers **a** and **b** then **a - b** is possible only if:
 $a \geq b$

Practice

Complete using \in or \notin

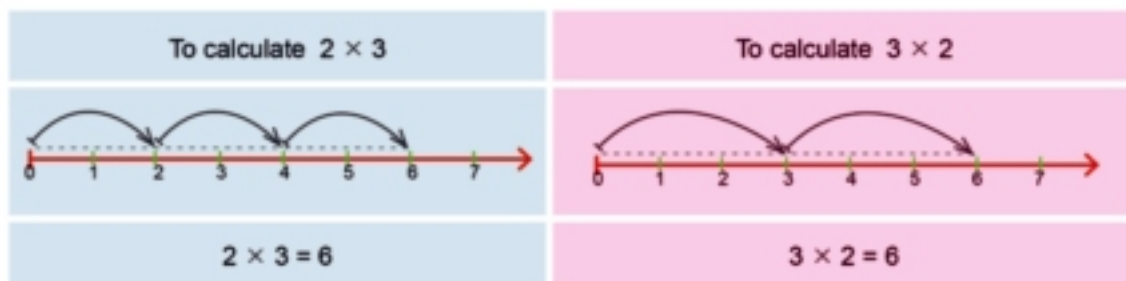
A $(3 + 7) \dots N$

B $(45 - 35) \dots N$

C $(8 - 10) \dots N$

D $(28727 - 9543) \dots N$

III : Multiplication operation in \mathbb{N} .



i.e. $2 \times 3 = 3 \times 2 = 6$

In general:

For any two natural numbers a and b :

$$a \times b = b \times a$$

Commutative property of multiplication in \mathbb{N}

Remarks

1. For any two natural numbers a and b : $a \times b = c$, $c \in \mathbb{N}$
i.e. the product of two natural numbers is a natural number.
i.e. closure property of multiplying in \mathbb{N} .
2. For $a \in \mathbb{N}$: $a \times 1 = 1 \times a = a$. For example, $5 \times 1 = 1 \times 5 = 5$
1 is called the multiplicative neutral element of multiplication in \mathbb{N} .
3. $(2 \times 3) \times 5 = 6 \times 5 = 30$, $2 \times (3 \times 5) = 2 \times 15 = 30$
i.e. $(2 \times 3) \times 5 = 2 \times (3 \times 5) = 2 \times 3 \times 5$
In general : For any natural numbers a , b and c
$$(a \times b) \times c = a \times (b \times c) = a \times b \times c$$

Associative property of multiplication in \mathbb{N} .
4. If $a \in \mathbb{N}$, then: $a \times 0 = 0 \times a = 0$

5 $2 \times (4 + 7) = 2 \times 11 = 22$, $2 \times 4 + 2 \times 7 = 8 + 14 = 22$

i.e. $2 \times (4 + 7) = 2 \times 4 + 2 \times 7$

In general. For any natural numbers a, b and c:

$$a \times (b + c) = a \times b + a \times c$$

also $(a + b) \times c = a \times c + b \times c$

Distributive property of multiplication over addition in N.



Complete :

A $5 \times (23 + 78) = 5 \times \dots + 5 \times \dots$
 $= \dots + \dots = \dots$

B $9 \times (24 + 17) = 9 \times \dots + 9 \times \dots$
 $= \dots + \dots$
 $= \dots$

IV: Division operation in N

$$6 \div 2 = 3 \quad , \quad 3 \in \mathbb{N}$$

While, $6 \div 5 = 1.2$, $1.2 \notin \mathbb{N}$

i.e. Division operation is sometimes not possible in N

Also $0 \div 5 = 0$, $0 \in \mathbb{N}$ because $5 \times \text{zero} = \text{zero}$

While $5 \div 0$ or $\frac{5}{0}$ is not possible because it is not defined. There is no number if multiplied by 0 produces 5.

Thus , dividing any natural number by zero is not possible.



Three natural numbers a , b and c , where $a = 12$, $b = 4$ and $c = 2$:

- A** Is $a + b$ equal to $b + a$?
- B** Is $a + b = c$, $c \in \mathbb{N}$?
- C** Is $(a + b) + c = a + (b + c)$?
- D** Is $c \times (a + b) = (c \times a) + (c \times b)$?

Exercises

1 Complete and tell the property used:

- A** $(4 \times 31) \times 25 = (31 \times \dots) \times 25$ Property
 $= 31 \times (4 \times \dots)$ Property
 $= 31 \times \dots = \dots$
- B** $2 \times (13 \times 5) = 2 \times (5 \times \dots)$ Property
 $= (2 \times \dots) \times 13$ Property
 $= \dots \times 13 = \dots$
- C** $7 \times (98 + 3) = \dots \times \dots + \dots \times \dots$ Property
 $= \dots$ Property

2 Use \in or \notin

- A** $\frac{0}{7}$ \mathbb{N}
- B** $(8 - 8)$ \mathbb{N}
- C** $\frac{3}{2-2}$ \mathbb{N}
- D** $(7 \times 3 - 3 \times 7)$ \mathbb{N}
- E** $(7 \times 2 - 7 \times 5)$ \mathbb{N}
- F** (0×9) \mathbb{N}

3 Complete to get a true sentence:

- A** The additive neutral element in N is whereas the multiplicative neutral element in N is
- B** If $9 \times 13 = 13 \times x$ then $x = \dots\dots\dots$
- C** $(93 + 87) - (87 + 93) = \dots\dots\dots$
- D** $7 \times 0 = \frac{\dots\dots}{9} = \dots\dots\dots$
- E** In the opposite figure: If m and n are two natural numbers, then $\dots\dots < \dots\dots$



4 Complete using:

(odd , even , prime , neither).

- A** An odd number + an even number = number
- B** The sum of two odd numbers = number
- C** An odd number \times an even number = number
- D** If x is an odd number , then $x + 2$ is number
- E** If x is an odd number , then $x - 1$ is number
- F** The smallest prime number \times any prime number = number.

5 Tell whether each statement is true or false:

- A** $(81 + 112) \times 117 = 117 \times (112 + 81)$ ()
- B** $(5 - 8) \in N$ ()
- C** $(28 + 6) \in N$ ()
- D** $5 - 0 = 0 - 5$ ()
- E** $(120 + 80) \times 4 = 120 \times 4 + 80 \times 4$ ()

- 6 Calculate using commutative, associative and distributive properties.
Check your answer using a calculator:

A $2 \times 347 \times 5$

B $4 \times 128 \times 75$

C $8 \times 49 \times 125$

D $10 (75 + 812 + 25)$

E $(125 \times 8 + 25 \times 40) \times 90$

- 7 If $a = 3$, $b = 4$ and $c = 0$, find the value of the following:

A $2 \times a + 5 \times b$

B $a \times c + b \times c$

C $(3 \times a + 5 \times b) \times c$

D $(a + b - c) \times (a + b)$

E $(b - a) (b + a)$

- 8 Let X be an even number between 3 and 8. Find the values of X then represent the values of $\frac{x}{2}$ on a number line.

- 9 Write the results of the given expressions in an ascending order.

$$7 \times 10 \quad , \quad 35 - 0 \quad , \quad 178 - 178 \quad , \quad (2 \times 3) \times 5$$

- 10 Complete the patterns :

A , 8, 11, 14,

B , 12, 24, 48,



Numerical Patterns

* You will learn *

- To complete numerical patterns.
- To make numerical patterns.



Key Terms

- A pattern
- A numerical pattern



Think and Discuss

In a math puzzle book, Hussam noticed an arithmetic triangle shown in the opposite figure. He and his friend FayeZ thought to complete the pattern through row 7. Can you help them?



Pascal Triangle

Example

Complete each of the following patterns:

A 5, 7, 9, 11,,

B 2, 6, 18, 54,,

C


D $1 \times 1, 2 \times 2, 3 \times 3, 4 \times 4, \dots, \dots$

Solution

A Remark: we started with 5 and to get the successive number, 2 is added. Therefore, the next two numbers are 13 and 15.

B Remark: we started with 2 and to get the successive number, we multiply by 3. Therefore, the next two successive numbers are $54 \times 3 = 162$ and $162 \times 3 = 486$



Remark: we started with one dot, then 4 and 9 dots. Therefore, the next successive number is as follows:  and consists of 16 dots.



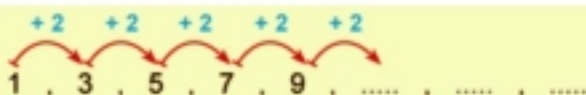
The next two successive numbers are 5×5 and 6×6 .



Practice

1

Complete using the same way:



3 , 33 , 333 , , ,



2 , 4 , 8 , , ,



1 , 4 , 7 , 10 , , ,



1 , 4 , 8 , 13 , , ,

2

Find the two successive numbers in each pattern:



2 , 7 , 12 , 17 , ,



1 , 3 , 9 , 27 , ,



5 , 15 , 25 , 35 , ,



7 , 77 , 777 , 7777 , ,

Exercises



- 1 Evaluate using a calculator . Write only 5 decimals without approximation.

$$\frac{1}{9} = 0.11111$$

$$\frac{2}{9} = \dots\dots\dots$$

$$\frac{3}{9} = \dots\dots\dots$$

Without using your calculator , can you evaluate:

$$\frac{4}{9} = \dots\dots\dots$$

$$\frac{5}{9} = \dots\dots\dots$$

$$\frac{6}{9} = \dots\dots\dots$$

$$\frac{7}{9} = \dots\dots\dots$$

$$\frac{8}{9} = \dots\dots\dots$$

- 2 Write down three successive numbers in each pattern:

A 142, 143, 145, 148, 152,

B 299, 293, 288, 282, 277,

C 480, 492, 486, 498, 492, 504,

D 106, 100, 94, 88, 82,

E 89, 79, 70, 62, 55,

- 3 Sherine sold a discount card that gives a discount to its owner at some fast food restaurants for LE 38. If the price of the card had increased LE4 annually during her owning to the card for 4 years. How much did she spend to buy this card?
- 4 Hany has 3 test rabbits in his lab. If the number of rabbits is doubled each certain period . How many rabbits will be there in 5 periods?

General Exercises

- 1 Find the sum using commutative and associative properties in \mathbb{N} . State the property used:

A $257 + 51 + 49$

B $77 + 651 + 49$

C $753 + 972 + 247$

D $892 + 788 + 308 + 512$

E $973 + 299 + 227 + 901$

- 2 Complete the table, where $a \in \mathbb{N}$ and a is greater than 6 :

Number	the number just before	the number just after	the number with 5 less
a
$a + 6$
$a + 5$
$a + 9$

- 3 A man is X years old , where $X \in \mathbb{N}$. Find :

A his age after 8 years .

B his age 15 years ago.

- 4 Write $<$, $>$ or $=$:

A $908 \dots\dots\dots 9008$

B $5075 \dots\dots\dots 5057$

C $2239 \dots\dots\dots 2229$

D $x + 18 \dots\dots\dots x + 17$, where $x \in \mathbb{N}$.

E $x - 18 \dots\dots\dots x - 17$, where x is a natural number greater than 20.

F $x \dots\dots\dots 75$ where $x \in \{ 30, 21, 32, 33 \}$.

G $y \dots\dots\dots 18$, where $y \in \{ 20, 21, 22, 23, 24 \}$

H $z \dots\dots\dots 35$, where $z \in \{ 35 \}$

- 5 Rewrite the following statements using $>$, \geq , $<$, or \leq :

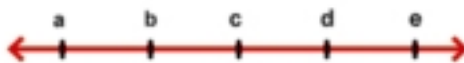
- A X is less than 8. B X is greater than 8.
 C 8 is less than X. D 8 is greater than 8.
 E Z is greater than or equal to L. F 9 is less than or equal to L.
 G 9 is greater than or equal to L. H Z is between 9 and 17.

- 6 Write the ascending order and the descending order of:

- A 85, 78, 79, 67, 74, 86, 25 B 453, 345, 435, 543, 354

- 7 In the opposite figure a, b, c, d and e are five natural numbers represented on a number line.

Complete using $>$ or $<$.



- A a c B d c C e b
 D e c E c a F d a

- 8 Represent the following sets on a number line:

- A $X =$ the set of natural numbers less than 7.
 B $Y =$ the set of natural numbers greater than 5.

- 9 a, b, c and d are four natural numbers where $d > a$, $b < c$, $c < d$, $b < d$, and $b > a$. Represent these numbers on a number line.

- 10 The greatest number of four consecutive natural numbers is $x + 7$. Find the other three numbers.

- 11 The greatest number of five consecutive natural odd numbers is $y + 15$. Find the other four numbers.

- 12 The middle number of three successive natural odd numbers is y . Find the other two numbers. What is the least value of the number y ?

13 Evaluate:

A $(16 + 24) \div 4$, $(16 \div 4) + (24 \div 4)$. What do you notice?

B $15 - 3 \times 6 \div 2 + 1$

C $8 \div (8 - 2 \times 3) + 3 \times 2$

14 Find the following products using the distributive property:

A 572×99

B 915×1001

C 45×99

15 Dina paid LE 34 for her annual membership card in a science club. Dina told her friend Hanaa that this amount is increased by LE11 annually. How much will it be after 10 years?

Activity

Notice each pattern then complete the next pattern:

1



2



3



4




Test

Unit test

1 Choose the right answer:

- A $75 + 89 = 89 + \dots$ (75, 100, 89)
 B The smallest natural number is $(0, \frac{1}{10}, 1)$
 C The next number in the pattern 5, 35, 65 is (70, 95, 105)

2 Complete each pattern :

- A 8, 16, 24,
 B 100, 85, 70,
 C  ,
 D $1 \times 2, 2 \times 4, 3 \times 8, \dots$

3 Evaluate using commutative and distributive properties :

- A 7×54 B $(12 + 98) \times 18$
 C $75 \times (198 + 802)$ D $125 \times 19 \times 8$

4 Complete to get a true sentence:

- A 99 added to the neutral element of multiplication =
 B $2358 \times 17 = 2358 \times (7 + \dots)$
 C $75 \times 99 = 75 (\dots)$
 $\quad \quad \quad = 75 \times \dots 75 \times \dots$
 D $\dots + 354 = 354$

Unit two

Equations

2



Mathematical Expressions



Think and Discuss

* You will learn *

😊 Numerical expression

😊 Algebraic expression



1 Numerical expressions

$$3 + 5 = 8 \quad , \quad 7 - 2 = 5$$

$$3 \times 7 = 21 \quad , \quad 21 \div 3 = 7$$

All previous expressions are known as numerical expressions.



2 Symbolic expressions

$$\square + 3 = 5$$

$$2 \times \square = 10$$

$$\triangle - 4 = 15$$

$$\frac{\bigcirc}{8} = \frac{3}{4}$$

The shape



can be replaced by the symbol

X



L



Z



Y

and the expression can be written as:

$$X + 3 = 5$$

$$2 \times Z = 10$$

$$L - 4 = 15$$

$$\frac{Y}{8} = \frac{3}{4}$$





These expressions are known as symbolic expressions.



Key Terms

- ▶ Numerical expression .
- ▶ Symbolic expression.





The following table summarizes it :

	Shape	symbol	Symbolic expression	Verbal expression (in words)
1		X	$X + 3 = 5$	Which number can be added to 3 to have the sum 5
2		L	$L - 4 = 15$	From which number 4 is subtracted to get 15
3		Z	$2 \times Z = 10$ or written as $2Z = 10$	Which number can be multiplied by 2 to have the product 10, or what is the number which if doubled, the result is 10
4		Y	$\frac{Y}{8} = \frac{3}{4}$	what's the value of Y that makes the fraction $\frac{Y}{8}$ equivalent to the fraction $\frac{3}{4}$

Remark $2 \times X$ is written as $2X$, $5Y$ means $5 \times Y$
 Also the double of X is written as $2X$. Also five times of Y is written as $5Y$



Complete using a suitable symbolic expression:

-  Add 6 to the number X, the symbolic expression is
-  Subtract 3 from the number Y, the symbolic expression is
-  Multiply 5 by the number Z, the symbolic expression is
-  Divide the number M by 3, the symbolic expression is

Exercises

1 Complete the following table as the example:

	Number	Add 3	Subtract 7	Multiply by 3	Divide by 4
Example	x	$x + 3$	$x - 7$	$3x$	$\frac{x}{4}$
A	y
B		$z - 7$
C		$\frac{L}{4}$

2 Complete the following table as the example:

	Verbal Expression (in words)	Symbolic Expression
Example	Add 3 to the double of the number x	$2x + 3$
A	Subtract 5 from the double of the number y
B	Add 7 to three times of the number z
C	Subtract 3 from the half of the number x	$\frac{1}{2}x$
D	Add 6 to one third of the number z

3 Complete:

- A Saeed has LE x and his father gave him LE8. How much will Saeed have?
- B The length of a rectangle is 3cm more than its width. Let the length be l cm, then the width will becm .

- C** The sum of what Manal and Nihal have is LE 10. If Manal has LE x , then Nihal will have LE.....

4 Choose a suitable symbolic expression:

- A** If we subtract 5 from the number X we get ($5x$, $5 - x$, $x - 5$, $x + 5$)
- B** Suzan saved LE x and her father gave her LE 10. She will have ... ($x - 10$, $x + 10$, $10x$, $10 - x$)
- C** Subtracting 3 from double of the number $x = \dots\dots(x - 3$, $2x - 3$, $3x + 2$, $5x)$
- D** The difference of two numbers is 7, and the smaller number is y , then the greater number will be = ($7y$, $7 - y$, $y - 7$, $y + 7$)

5 Translate into symbolic expressions:

- A** Subtract 8 from a number.
- B** Add 5 to the 3 times of a number.
- C** Add 4 to the half of a number.
- D** Subtract 7 from one third of a number.

6 Complete:

- A** The perimeter of a square whose side length is $\ell = \dots\dots\dots$
- B** The perimeter of a rectangle is 20 cm. If its length is x cm, then its width =
- C** The lengths of two adjacent sides of a parallelogram are x and y , then its perimeter =
- D** If the sum of two numbers is 10 and one of them is X , then the other =

The Constant and the Variable



Think and Discuss

* You will learn *

- 😊 The meaning of a constant
- 😊 The meaning of a variable
- 😊 The meaning of a mathematical relation



Key Terms

- ▶ Constant
- ▶ Variable
- ▶ Mathematical Relation

If the price of a pen is LE 2 complete:

the price of 3 pens = $3 \times 2 = \text{LE } 6$

the price of 4 pens = $4 \times \dots = \text{LE } \dots$

the price of 8 pens = $8 \times \dots = \text{LE } \dots$

the price of 12 pens = $\dots \times \dots = \text{LE } \dots$



Remark

In this example, the price of one pen is constant whereas the prices of pens vary according to variation in its number.

Let x represent the number of pens
and y represent the price of the pens, then y depends on x ,
the price of x pens.

$$y = 2 \times x \quad \text{or} \quad y = 2x.$$

Record the values of X and their corresponding values of Y in the following table:

x	3	4	8	12
y	6

Remark

The relation $Y = 2X$ relates the two variables X and Y and is called a **mathematical relation**.

Practice

The price of a meal in a restaurant is LE 15, and LE 3 are added for delivery service, it does not matter, how many meals.



How much should be paid in the following cases?

- A 1 meal house delivery you pay LE..... .
- B 3 meals house delivery you pay LE
- C 4 meals house delivery you pay LE

Remark Total price = a meal price \times the number of meals + delivery service

Let y represent the total price you have to pay and x the number of meals you order, then the relation between y and x is as follows:

$$y = \dots\dots\dots$$

Remark The number of meals is the variable and is denoted by X .

The total price is the variable and is denoted by Y .

The price of one meal is the constat.

and the price of delivery service is the constant .



Practice

- 1 An isosceles triangle with base 5cm. Find the mathematical relation between the lengths of its sides and its perimeter .
Let P represent the perimeter of the triangle ABC and L represent the length of AC

then $AC = \dots\dots\dots$

the perimeter of the triangle $ABC = \dots\dots + \dots\dots + \dots\dots$

$$P = 2L + 5 \text{ cm.}$$



Remark

The lengths of AB and AC are variables, while the length of the base BC is constant and equals 5 cm.



Practice

The owner of a factory pays the daily wage of one of his workers according to the mathematical relation $Y = 12 + 5X$
Where X represents number of working hours done in overtime and Y represents the daily wage in LE .



Complete:

The constant daily wage = LE $\dots\dots\dots$.

The constant daily wage and overtime-wage = LE $\dots\dots\dots$.



Complete the following table that shows the mathematical relation of the daily wage according to the overtime hours:

Number of over time hours (x)	0	1	2	5
Total daily wage (y)	27	32



Exercises

1 Choose the right answer:

- A The side length of an equilateral triangle is L and its perimeter is P . The mathematical relation between P and L is : $P = \dots\dots (\frac{1}{3} L, L + 3, 3 L, L - 3)$
- B The length side of a rhombus is x and its perimeter is P . The mathematical relation between P and X is : $P = \dots\dots (4x, x + 4, x - 4, x + 4)$
- C If the sum of two numbers x and y is 20 , then $y = \dots\dots$
 $(20 + x, 20 - x, x - 20, \frac{x}{20})$
- D x and y are two numbers. The greater number is 3 more than the other. If the smaller number is y , then $x = \dots\dots (3y, y - 3, y + 3, \frac{1}{3} y)$

2 If $y = 4x$ is the mathematical relation between x and y , then complete the table:

x	3	1	5
y	24	16	28

- 3 Write down the mathematical relation between x and y , if the number x is 9 more than the double of y .
- 4 Medhat bought x kg of chocolate and put it in a box that costs LE5. Calculate what Medhat should pay in terms of x if the price of 1 Kg of chocolate is LE 28.



Equations



Think and Discuss

* You will learn *

- ☺ The meaning of an equation
- ☺ To solve an equation



Key Terms

- ▶ Balance or equality
- ▶ Equation
- ▶ Solving an equation



1 The meaning of the equation

Observe and look for the answer:



If the scale is balanced, then



Weight of =



Weight of =

If the weight of a rabbit is x kg, then the mathematical relation $x + 3 = 5$ describes the balanced situation of the scale, and this mathematical relation is called an equation.

In the second case, if the watermelon weighs y kg, then the equation is $y + 2 = 5$ and is called an equation.

Practice

1 Complete :

	Verbal expression	Symbolic expression
Example	Adding 3 to a number produces 11	$x + 3 = 11$
1	Adding 7 to a number produces 15
2	Subtracting 2 from a number produces 33
3	Adding 5 to the double of a number produces 17
4	Subtracting 9 from the double of a number produces 23

2 Sohair saved LE 14. She bought 3 copybooks, with the price of LE X for each one and LE 8 remained with her.

Choose a suitable equation for this situation

A $14 + 3x = 8$

B $8 - 3x = 14$

C $3x + 8 = 14$

D $3x - 14 = 8$



Think

1 The equation $50 + x = 86$ may represent the following real world situation:

The distance between two cities is 86 km. A car covered this distance in two stages. The first stage was 50 km and the rest was covered in the second stage. Tell another real life situation that can be represented by the same equation.



2 Write a real life situation for each equation:

A $x + 10 = 28$

B $2y - 15 = 7$

C $8 + 3y = 23$

D $2x - 3 = 11$

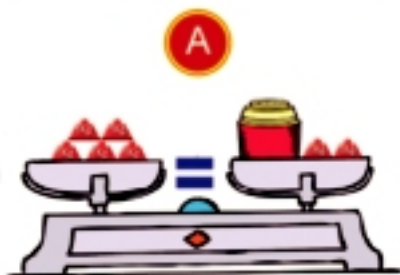


Examine the opposite figure and discuss it with your group.

In figure **A** the scale is balanced.

☺ Take away two units from each pan as shown (in figure **B**) Does the scale keep balanced?

☺ Add three units to each pan. Does the scale keep balanced? What do you deduce?



Remark

Adding (or subtracting) equal amounts to (or from) both sides does not affect on the equality of the equation.

2

Solving Equations

Example

Find the number which if added to 3, the sum is 9.

Remark

The variable is an unknown number (its value is unknown). Therefore, x is used to express it and the equation that describes this statement is :

$$x + 3 = 9$$

Now: Can you solve this equation and find the value of the unknown x ?

Solving an equation: It is to find the value of the unknown (symbol) included in the equation.

Solution

To solve $x + 3 = 9$ we have to look for a number if added to 3, the sum is 9 i.e.: $x + 3 = 9$ is the same as : $6 + 3 = 9$ therefore, $x = 6$.

Another solution:

$x + 3 = 9$ Subtracting 3 from each side as it doesn't affect the equality.

$$x + 3 - 3 = 9 - 3$$

Thus : $x = 6$



Solve the equation $x - 5 = 8$

(Add 5 to both sides) $5 + x - 5 = 5 + 8$ (because adding a constant number to both sides has no effect on the equation equality).

$$x + 5 - 5 = 5 + 8 \text{ (Commutative property).}$$

So, $x + \text{zero} = \dots\dots\dots$ (Additive neutral element).

Thus: $x = \dots\dots\dots$

Exercises

In each of the following figures, the two pans of the scale are balanced as in the first case:

1



Equation: $x + 9 = 11$

Solution: $x = 2$

2



Equation:

Solution:

3



Equation:

Solution:

4



Equation:

Solution:

General Exercises

1 Translate each verbal statement into an equation :

- A A number if added to 17 the sum is 28.
 B If 9 is subtracted from a number, then the result is 23.
 C If 5 is subtracted from 3 times of a number , then the result is 16.

2 Write down a real-life situation that represents each of the following equations:

- A $x + 7 = 29$ B $x - 5 = 19$ C $3y + 9 = 18$

3 Solve each equation:

- A $x + 3 = 12$ B $2x - 6 = 10$ C $x - 7 = 25$
 D $y - 5 = 7$ E $9 + y = 44$

4  Mental Math

(1) Find the value of X in the following:

- A $22 + x = 9 + 22$ B $35 + x = 18 + 35$
 C $7x = 117 \times 7$ D $12 \times (17 \times x) = (12 \times 17) \times 32$
 E $3 \times 52 = (x \times 2) + (x \times 50)$ F $(7 \times 9) + (x \times 5) = 7 \times 14$

(2) Solve each of the following equations.

- A $24x = 61 \times 24$ B $6 \times 14 = 6 \times (x + 5)$
 C $8 \times 45 = x(35 + 10)$ D $(x + 2) \times 7 = 7 \times 8$
 E $573 = x + (7 \times 10) + (5 \times 100)$ F $482 = (4 \times x) + (8 \times 10) + 2$
 G $42 = 2 + x \times 10$ H $x \times 7 + x \times 50 = 2 \times 57$

Technology



Applications on natural numbers and equations using Excel-program:

Practice: **Evaluate** : $252 \times 76 + 252 \times 24$

To solve the problem: There are two possible ways to evaluate the numerical expression:

First way: open your Excel program:

- 1 Enter the number 252 on cell A_1 ,
- 2 Enter the number 76 on cell B_1 ,
- 3 Enter the number 24 on cell C_1 ,
- 4 Do a mouse click on E_1 and write down = then $A_1 \times B_1$ then press **Enter** the product of: 252×76 is 19152.
- 5 Repeat the same steps 1 - 4 : do a mouse click on G_1 and write down = then $A_1 \times C_1$, then press **Enter** the product of : 252×24 is 6048.
- 6 Do a mouse click on I_1 and write down = then $(E_1 + G_1)$, then press **Enter** the final result is 25200



Second way:

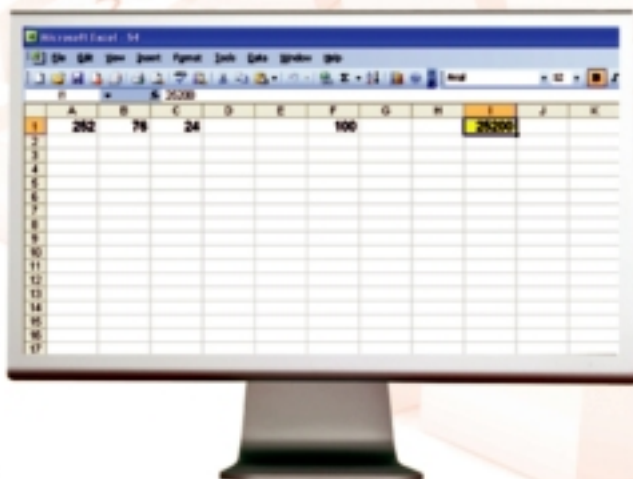
To evaluate $252(76 + 24)$

Where:

$[252 \times 76 + 252 \times 24 = 252 \times (76 + 24)]$ (Give reason for your answer)

To solve the problem: open excel program and repeat steps

- 1, 2, 3 mentioned previously.
- 4 Do a mouse click on cell F_1 then =, and write $B_1 + C_1$ then press **Enter** the sum of $(76 + 24)$ is 100



- ⑤ Do a mouse click on I_1 and write $=$ then $A_1 \times F_1$, then press **Entre** the final result is 25200.

Compare the results in these two ways and be sure of the equality.

Evaluate the following numerical expressions using Excel Program (in two different ways):

- (1) $225 \times 98 - 205 \times 98$
 (2) $95 \times 98 + 95 \times 402$
 (3) $39 \times 52 + 39 \times 8 + 39 \times 40$

Solve for X: $2X + 3 = 11$

Solution:

- ① Open Excel program and enter the variable x on cell A_1 .
- ② Do a mouse click on cell A_2 and enter the number 1, do a mouse click on cell A_3 and enter the number 2 and continue till you reach the last cell which is number 6 then leave the mouse.
- ③ Do a mouse click on cell B_1 and enter $3 + 2x$.
- ④ Do a mouse click under cell B_1 enter $=$ then $2 \times A_2 + 3$ (A_2 represents the number 1) and then press **Enter** the result is 5.
- ⑤ Without doing any calculation, press on cell B_2 , a little square will appear on the left end. Do a mouse click on this square and drag it down till the end of the cell reached, where evaluations should be done, then leave the mouse.

	A	B	C	D	E	F	G	H	I	J	K
1	x	$2x+3$									
2	1	5									
3	2	7									
4	3	9									
5	4	11									
6	5	13									
7	6	15									
8											
9											
10											
11											
12											
13											
14											

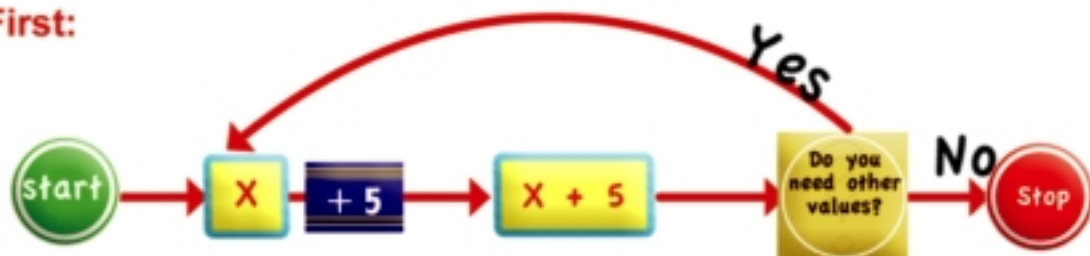
The solution: The number 11 highlighted on the cell B_5 satisfies the right side of the equation. Therefore, the solution of the equation. $2X + 3 = 11$ is $X = 4$

Use Excel program and solve for X: $2(3X + 4) = 38$

Activity

Ahmed wants to innovate some exercises about numerical patterns to prepare puzzle games among school classes . He designed the following successive diagrams:

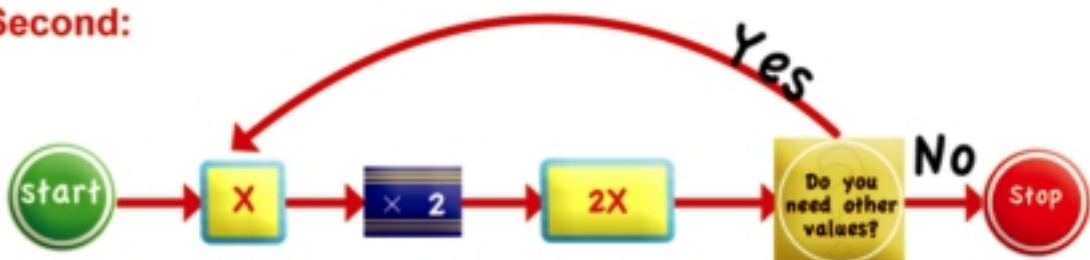
First:



Choose any value for the variable X , let it be 7 and follow the instructions given in the shown pattern above. For instance : $7 + 5 = 12$ to complete the pattern, enter 12, then add 5 to get 17 and so on.

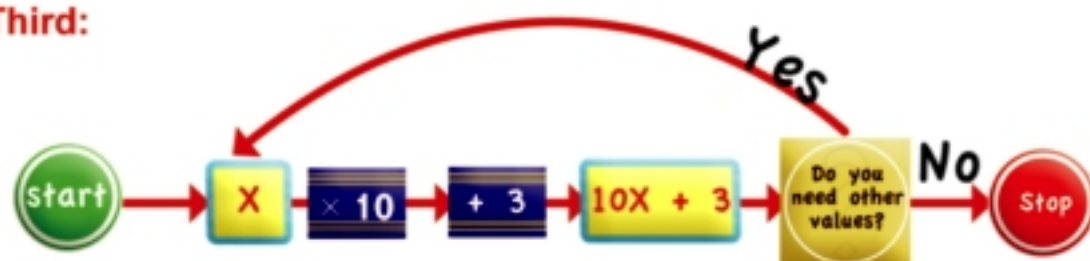
Complete : 7, 12, 17,,

Second:



Complete the pattern : 4,,,,

Third:



Complete the pattern : 3,,,,

Can you help Ahmed design other new patterns?

Test

Unit test

1 Translate the verbal statements into symbolic expressions.

- A 7 is added to the double of a number.
- B 3 is subtracted from three times of a number.

2 Complete:

- A The perimeter of a square whose side length is x =
- B The perimeter of an equilateral triangle whose side length is l =
- C The area of a rectangle whose length is x cm and width is 5 cm = cm^2

3 Solve the following equations:

- A $x + 5 = 7$
- B $y - 3 = 9$
- C $3 + x = 11$

4 Write down a real life situation that can be represented by the equation $x + 5 = 12$, then solve for x .

5 Solve for X :

$$75 = 5x + 7 \times 10$$

Unit three

Measurement

3



π



Area and its Units



Think and Discuss

* You will learn *

- ☺ Area measuring unit
- ☺ To find area of a surface
- ☺ To find area of a triangle



Key Terms

- ▶ Area
- ▶ Base
- ▶ Height
- ▶ Square centimeter
- ▶ Square meter
- ▶ Square kilometer
- ▶ Square decimeter
- ▶ Congruent surfaces

Remember

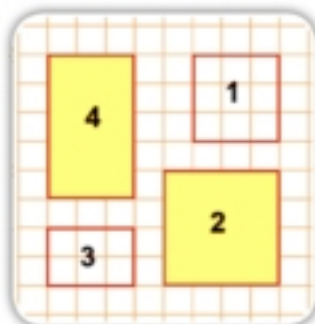
Area of a rectangle =
length \times width.

Area of a square =
side length \times itself.

You have studied before the area and perimeter of some geometric shapes. You know that the perimeter is the distance around a shape.

Area of any surface = number of units needed to cover a flat surface.

Now observe the opposite figure and calculate the number of square units which express the area of each shape and complete:



Number and name of shape	Area in Square units
(1) Square	9
(2)
(3)
(4)

Remember the area measuring units:

A 1 Square cm = $1\text{cm}^2 = 100\text{mm}^2$

this is the area of a square whose side length is 1 cm

1 cm



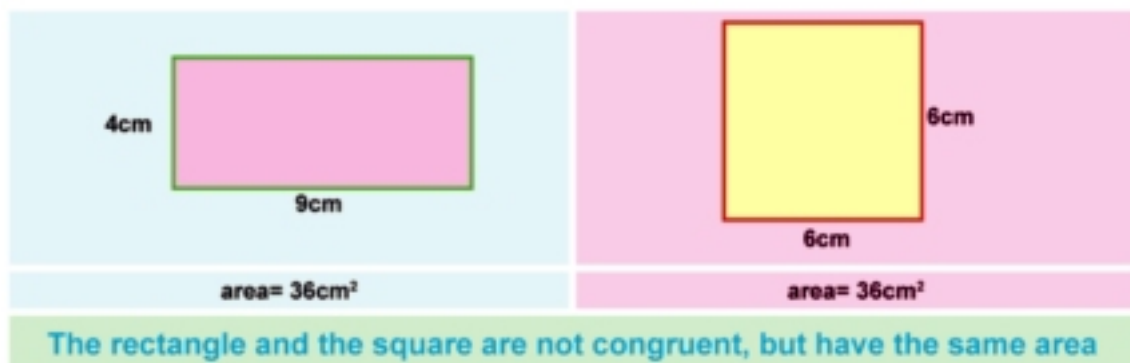
B 1 Square meter (1m^2) = $100 \times 100 = 10000\text{cm}^2$

C 1 Square kilometer (1km^2) = $1000 \times 1000 = 1000\,000\text{m}^2$

D 1 Square decimeter = (1dm^2) = $10 \times 10 = 100\text{cm}^2$

Area of any surface = Sum of areas of the parts forming this surface

Remark



Congruent shapes have the same surface area but the converse is not always true.

Areas of Triangles



Let's work together.

Write the area of the colored part where  represents 1cm^2



area of the rectangle = 3cm^2

area of the colored triangle

= $\frac{1}{2}$ area of the rectangle

= $\frac{1}{2} \times 3 = \frac{3}{2}\text{cm}^2$



area of the rectangle = cm^2

area of the colored triangle = cm^2



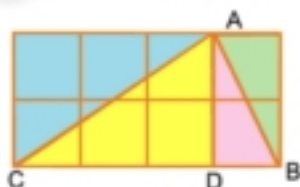
area of the rectangle = cm^2

area of the colored triangle = cm^2



area of the rectangle = cm^2

area of the colored triangle = cm^2



Area of $\triangle ABD = \dots \text{cm}^2$

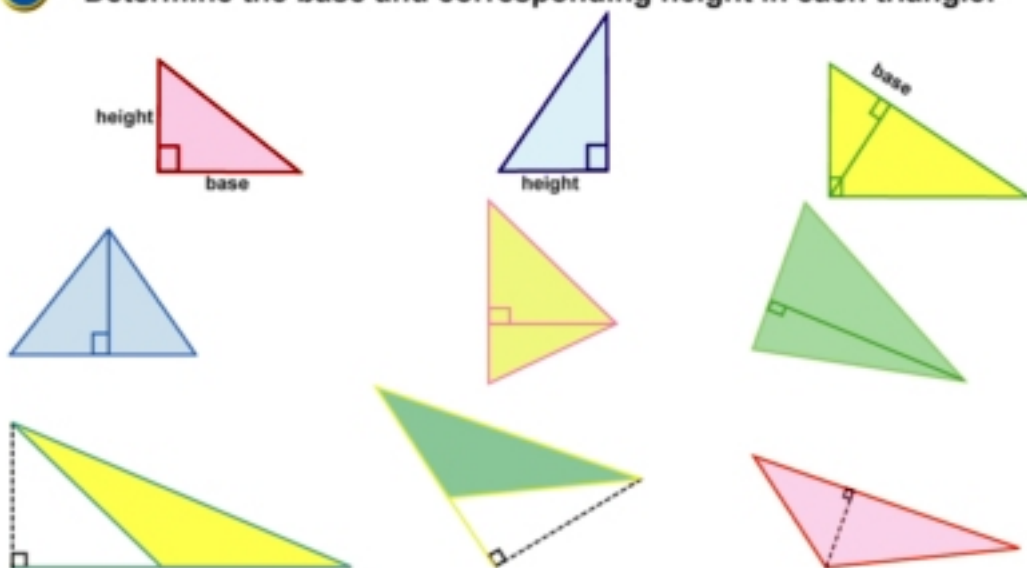
Area of $\triangle ADC = \dots \text{cm}^2$

Area of $\triangle ABC = \dots \text{cm}^2$

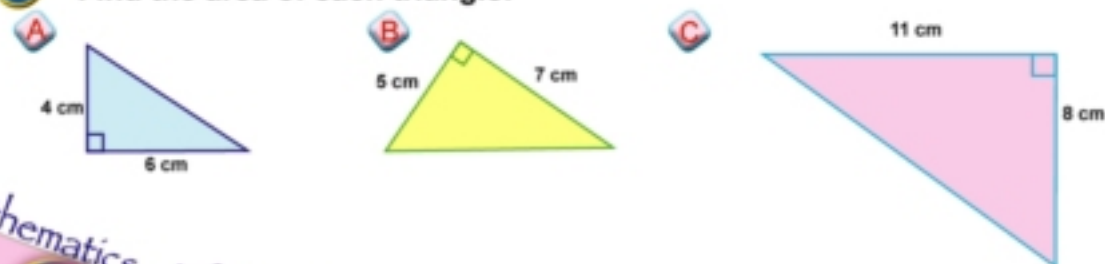
Area of the triangle = $\frac{1}{2}$ the length of its base \times its height

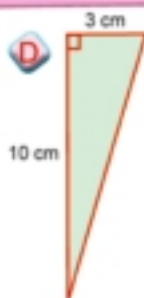
Practice

1 Determine the base and corresponding height in each triangle:



2 Find the area of each triangle:





3 Complete the table:

Base length of \triangle (cm)	Height of \triangle in (cm)	Area of \triangle in (cm ²)
12	9
10	25
.....	8.2	24.6

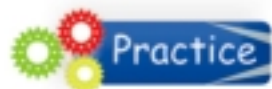
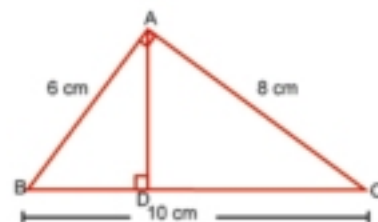
4 In the opposite figure:

$\triangle ABC$ is a right angled triangle at A,

$\overline{AD} \perp \overline{BC}$. Complete:

The area of $\triangle ABC = \frac{1}{2} \times 8 \times \dots = \dots \text{cm}^2$

also the area of $\triangle ABC = \frac{1}{2} \times 10 \times AD = 5 \times AD$, then $AD = \dots \text{cm}$



In the opposite figure, $ABCD$ is a rectangle whose area is 828 cm²,

$E \in \overline{BC}$, $AD = 23 \text{ cm}$ and $BE = 35 \text{ cm}$. Find the area of $\triangle DCE$

Solution:

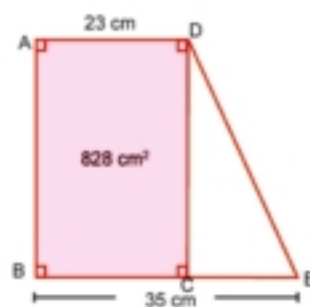
The area of the rectangle $ABCD = 23 \times AB$

$$828 = 23 \times AB$$

$$AB = \frac{828}{23} = \dots \text{cm}$$

$$DC = \dots \text{cm}, CE = 35 - \dots = \dots \text{cm}$$

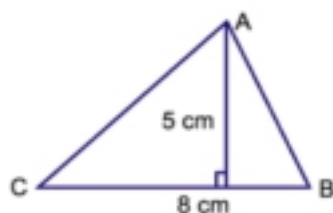
$$\text{The area of } \triangle DCE = \frac{1}{2} \times \dots \times \dots = \dots \text{cm}^2$$



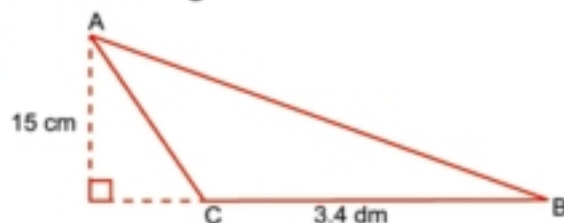
Exercises

- 1 Find the area of $\triangle ABC$ in each of the following:

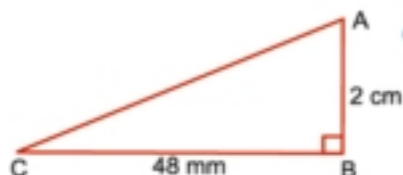
A



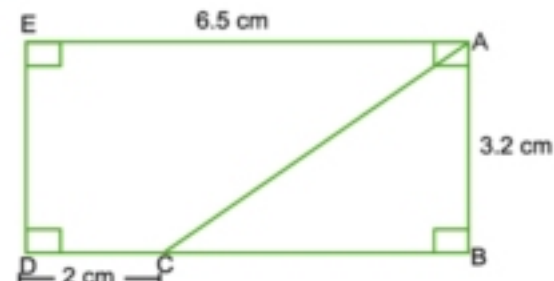
B



C

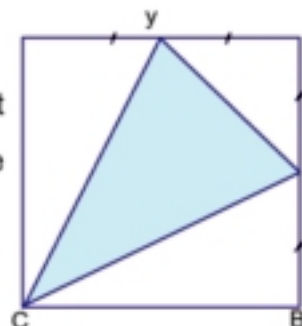


D



- 2 In the opposite figure:

The side length of the square $ABCD$ is 8 cm , X is the midpoint of \overline{BA} , Y is the midpoint of \overline{DA} . Find the area of the three non colored triangles, then conclude the area of $\triangle XCY$.



- 3 Which area is greater: a triangle with base $= 3.25\text{ dm}$ and height $= 4\text{ dm}$ or a rectangle with dimensions of 26 cm and 20 cm ? Find the difference in cm^2 .

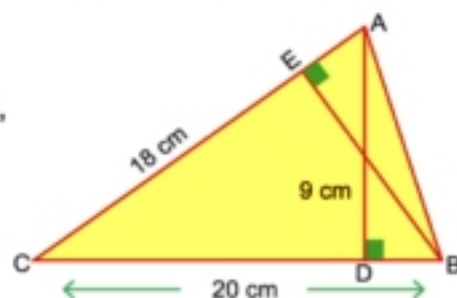
- 4 In the opposite figure, find :

A

The area of $\triangle ABC$, where $AD = 9\text{ cm}$,
 $AC = 18\text{ cm}$, $BC = 20\text{ cm}$

B

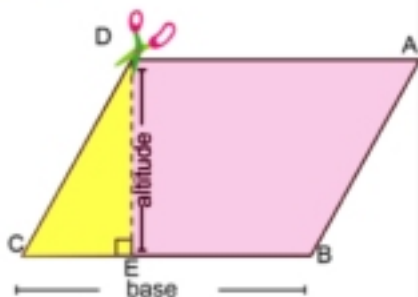
The length of \overline{BE}



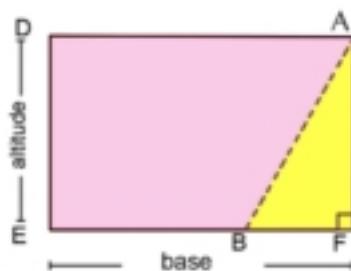
Area of Parallelogram

Activity

- 1 Cut the parallelogram ABCD from a piece of paper in a way the parallelogram is congruent to the figure opposite. From its vertex D, draw an altitude to the opposite side \overline{BC}



- 2 Separate the triangle DEC and place it in the position of the triangle AFB.



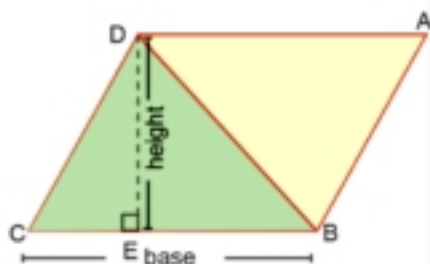
What is the name of the formed figure AFED? Complete: the area of the parallelogram ABCD = The area of

Area of a parallelogram = base \times height

Check:

You know the diagonal of a parallelogram divides it into two congruent triangles.

$$\begin{aligned} \text{Area of parallelogram} &= \\ &= 2 \times \frac{1}{2} \text{ base} \times \text{height} \end{aligned}$$



Area of a parallelogram = base \times height

* You will learn *

- To find the area of a parallelogram.

Key Terms

- ▶ Parallelogram
- ▶ Base of a parallelogram
- ▶ Height of a parallelogram

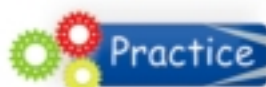
Remark

An altitude of a parallelogram is a perpendicular line segment from a line containing the base to a line containing the side opposite the base. Any one of these sides is called a corresponding base.



How many altitudes are there in a parallelogram?

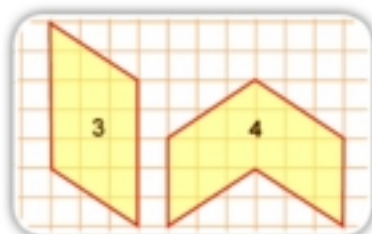
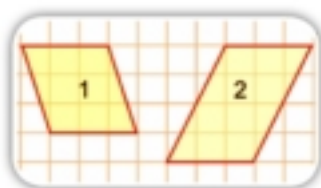
When do the altitudes equal in the parallelogram?



- 1 In each figure of the following, determine the base of the parallelogram and its corresponding height.



- 2 Complete to find the area of the colored figures:



Area of figure 1 = \times = square units.

Area of figure 2 = \times = square units.

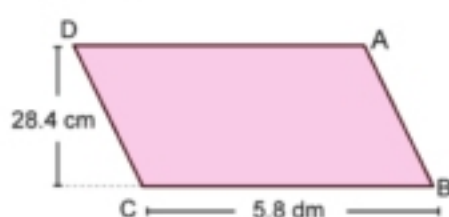
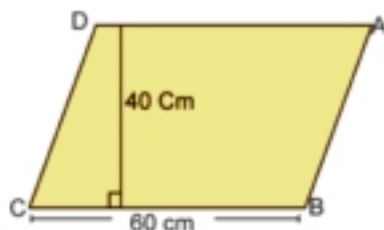
Area of figure 3 = \times = square units.

Area of figure 4 = + = square units.

- 3 Complete the table for parallelograms:

Length of the base in cm	Height in cm	The area in cm^2
8	3.25
6.1	54.9
.....	4.2	63

- 4 Find the area of each parallelogram in each figure.

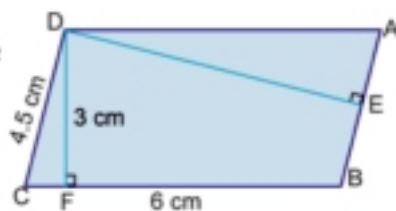


- 5 In the opposite figure, complete:

Area of the parallelogram $ABCD = BC \times DF = \dots \text{cm}^2$

also, area of the parallelogram = $\dots \times DE$

deduce the length of DE .

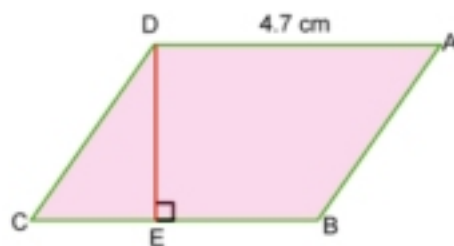


Exercises

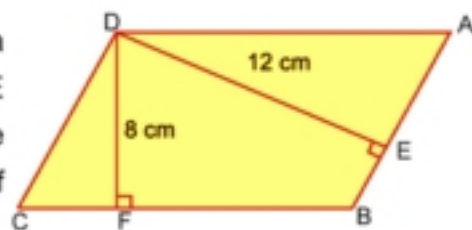
- 1 Choose the correct answer :

In the opposite figure, the area of the parallelogram is:

- A 13.63 cm B 7.6 cm^2
 C 13.63 cm^2 D 12.63 cm^2



- 2 In the opposite figure, $ABCD$ is a parallelogram in which $AB = 10\text{cm}$, $DE = 12\text{cm}$, $DF = 8\text{cm}$. Find the area of the parallelogram $ABCD$, then find length of BC .



- 3 In the opposite figure: Complete, A B C D is a parallelogram where,

$$B C = 12 \text{ cm},$$

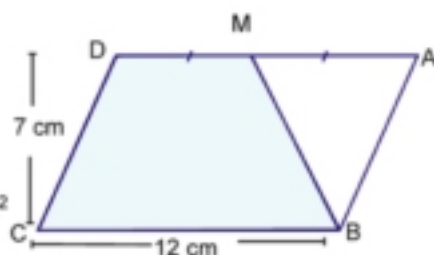
$$A D = \dots \text{ cm}$$

$$A M = \dots \text{ cm}$$

$$\text{the area of the parallelogram A B C D} = \dots \text{ cm}^2$$

$$\text{the area of the triangle A B M} = \dots \text{ cm}^2$$

$$\text{the area of the figure M B C D} = \dots \text{ cm}^2$$

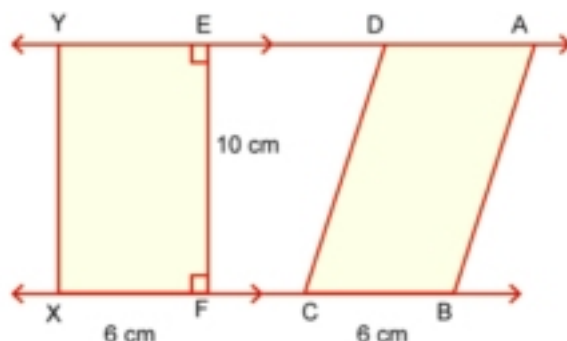


- 4 Find to the nearest hundredth, the area of a parallelogram whose base length is 34.7 cm and height 28.17 cm.

- 5 Which area is greater: the area of a parallelogram whose base length is 15.7 cm and height 9.4 cm, or the area of a triangle whose base length is 14 cm and height 18 cm?

- 6 In the opposite figure, $\overleftrightarrow{AY} \parallel \overleftrightarrow{BX}$
A B C D is a parallelogram and E F X Y
is a rectangle.

Compare the area of the parallelogram
and the area of the rectangle.



- 7 **Patterns:** Khaled drew parallelograms this way: the first with base length = 2 cm and height = 2 cm, the second with base length = 2 cm and height = 4 cm, the third with base length = 2 cm and height = 8 cm, and continued with this pattern. Find the area of the eighth parallelogram according to his pattern.

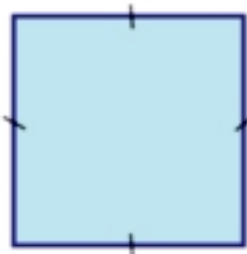
Area of a square in terms of its diagonal length



Think and Discuss

You have learned before:

the area of a square = side length \times itself



For example: to find the area of a square whose side length is 5 cm, then

the area of the square = $5 \times 5 = 25 \text{ cm}^2$



Find the area of a square whose side length is 2.7 cm?

Now, you will learn to find the area of a square in terms of its diagonal length.

Area of a square = $\frac{1}{2}$ diagonal length \times diagonal length

Remark

The lengths of the diagonals of a square are equal in length.

Example

Find the area of a square whose diagonal length is 8 cm.

Solution:

$$\begin{aligned} \text{Area of the square} &= \frac{1}{2} \text{ diagonal length} \times \text{diagonal length} \\ &= \frac{1}{2} \times 8 \times 8 = 32 \text{ cm}^2 \end{aligned}$$

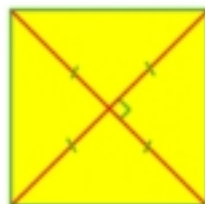
* You will learn *

To find the area of a square in terms of its diagonal length.

Key Terms

▶ Diagonal of a square

Remember



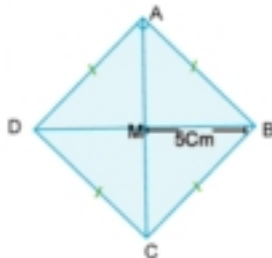
The diagonals of a square are:

- (1) Equal in length.
- (2) Perpendicular to each other.
- (3) Bisecting each other.

Practice

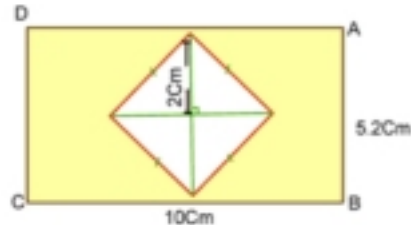
- Find the area of a square whose diagonal length is 16 cm.
- Complete:

A



$BM = 5 \text{ cm}$
 the diagonal length $\overline{BD} = \dots \text{ cm}$
 the area of the square ABCD = $\dots \text{ cm}^2$

B



The area of the rectangle = $\dots \text{ cm}^2$
 the area of the square = $\dots \text{ cm}^2$
 the area of the colored surface = $\dots \text{ cm}^2$

Exercises

- The diagonal length of a square is 6 cm. Find its area.
- The area of a piece of paper is 312.5 cm^2 if 7 congruent squares with diagonal lengths of each 9 cm are cut off. Find the area of the left part of the paper.
- A square shaped piece of land with diagonal length 28 m. A square shaped house with side length 15 m has been built on it and the left part was used as a garden . Find the area of the garden.

Garden

House

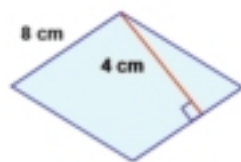
The Area of a Rhombus in terms of its Diagonal lengths



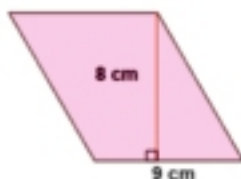
Think and Discuss

You have learned before that a rhombus is a parallelogram. Therefore, to find its area, the same rule to find the area of a parallelogram is used.

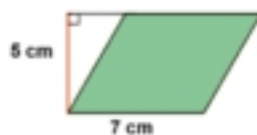
Find the area of each rhombus:



area = ... cm^2



area = ... cm^2



area = ... cm^2

Now, you will learn to find the area of a rhombus in terms of its diagonal lengths.

Area of a rhombus = $\frac{1}{2}$ the product of its diagonal lengths.



Practice

Observe the opposite figure and calculate the area of each rhombus in terms of its diagonal lengths. Figure (1) is given as an example.

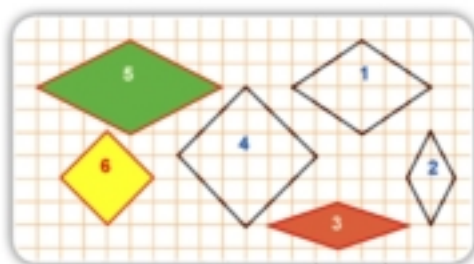


Figure number	Area in Square units	Figure number	Area in Square units
1	$\frac{1}{2} \times 4 \times 6 = 12$	4
2	5
3	6

* You will learn *

- To find the area of a rhombus in terms of its diagonal lengths.

Key Terms

- Rhombus
- Diagonal of a rhombus

Remember

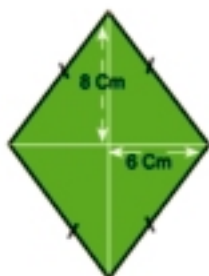
The diagonals of a rhombus are:

- (1) Perpendicular to each other
- (2) Bisecting each other

Exercises

1 Find the area of each figure:

A



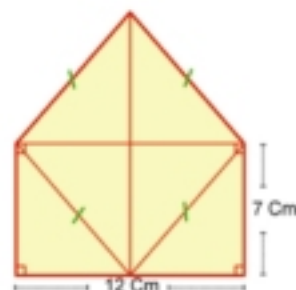
area = cm^2

B



area = cm^2

C



area = ... cm^2

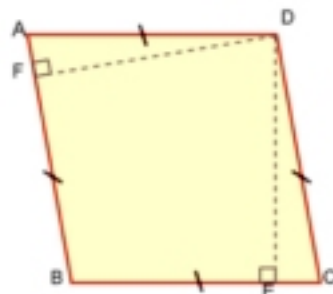
2 Complete the following table:

Diagonal length of rhombus	The other diagonal length of rhombus	Area of rhombus in square units
3 cm	5.4 cm cm^2
2.3 cm cm	4.6 cm^2
24 mm	3 cm mm^2
27 cm dm	8.1 dm^2
1.7 m cm	3.4 m^2

3 In the opposite figure, find:

- a) The area of the rhombus ABCD, whose side length is 10 cm and diagonal lengths are 16 cm and 12 cm.
 b) The length of \overline{DE} , and \overline{DF} .

What can you say about the heights of rhombus?



4 Find the area of a rhombus with diagonal lengths 7 cm and 9 cm and if its height is 5 cm. Find its side length.

Circumference of a Circle

Activity 1

Find using a measuring tape:

- The length of the curved line that represents a circle located at the middle of a football playground. The length of this curved line is called the circumference of the circle.

Circumference of the circle =



- Measure the length of the diameter of this circle.
Diameter length =

- Find $\frac{\text{circumference of the circle}}{\text{diameter length of the circle}} = \dots\dots\dots$

Activity 2

Ahmed made a sign on the front wheel of his bicycle, where it touches the earth. He labeled the touch point A on the earth. Then he rode his bicycle in a straight line till the sign touched the earth again and labeled it B on the earth. He recorded the following data:

Circumference of the wheel = the length of \overline{AB} =

Diameter length of the wheel =

Find $\frac{\text{circumference of the circle}}{\text{diameter length of the circle}} = \frac{\dots\dots\dots}{\dots\dots\dots} = \dots\dots\dots$



* You will learn *

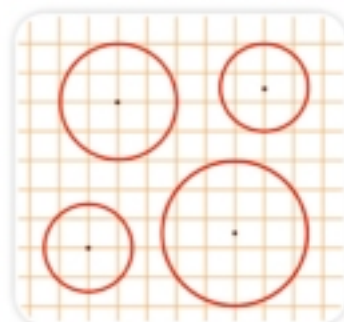
- To find the circumference of a circle.
- What is the approximate ratio π ?

Key Terms

- Circumference of a circle
- The approximate ratio π .

Activity 3

Use a compasses to draw some circles with different radii as shown in the opposite figure. Find the circumference of each circle using a fine thread.



Record the results in a table like the following one:

Diameter length	Circumference	$\frac{\text{circumference}}{\text{diameter length}}$
.....
.....
.....
.....

Use a calculator to do the division operation. What do you notice?

From activities 1, 2 and 3 we observe that:

$\frac{\text{circumference}}{\text{diameter length}}$ has nearly the same value and approximately equal to 3.14 or $\frac{22}{7}$

and known as approximate ratio π and pronounced "pie".

Mathematician Ghiatho Al-dein Alkashi, 1380 - 1436 B.C, calculated an approximate value for this ratio.

i.e. : $\frac{\text{circumference of a circle}}{\text{diameter length of the circle}} = \pi$

The circumference of a circle = $\pi \times \text{diameter length}$

Where $\pi \approx 3.14$ or $\frac{22}{7}$

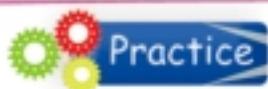
Example

Find the circumference of a circle with diameter length 14 cm.

Solution:

The circumference of a circle = $\pi \times \text{diameter length}$

$$= \frac{22}{7} \times 14 = 44 \text{ Cm}$$



Complete the table :

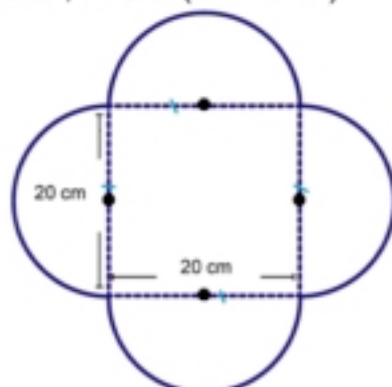
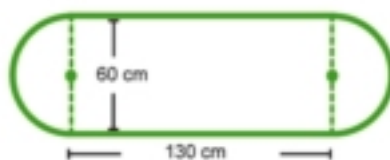
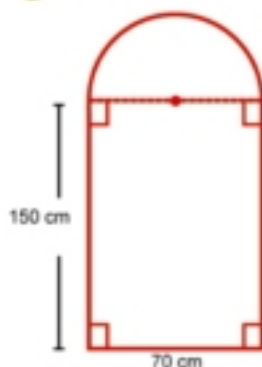
Radius length	Diameter length	π	Circumference
7 cm	...cm	$\frac{22}{7}$ cm
..... cm	20 cm	3.14
..... cm cm	3.14	75.36 cm
mm	98 mm	$\frac{22}{7}$	mm



- Find the circumference of the following circles whose radii lengths are:
($\pi = \frac{22}{7}$) for each.
 - 48 cm
 - 14 cm
 - $10\frac{1}{2}$ cm
 - 3.5 cm
- Find the circumference of the following circles whose diameters lengths are:
($\pi = 3.14$) for each.
 - 10 cm
 - 100 cm
 - 50 cm
- Find the radii lengths of the following circles whose circumference are:
($\pi = \frac{22}{7}$) for each.
 - 88 cm
 - 11 cm
 - 66 cm
- Two circles in which the diameter length of the first one is 20 cm and 40 cm for the other. Find the difference between their circumferences. ($\pi = 3.14$)
- If the wheel's diameter length is 66 cm. What is the distance that the bike covers if the wheels turns 1000 rounds. ($\pi = 3.14$)

General Exercises

- 1 Calculate the circumference of a circle whose diameter length is 15.4 cm to the nearest hundredth (where $\pi = 3.14$)
- 2 Calculate the perimeter of each of the following figures, where ($\pi \approx 3.14$)



- 3 A wheel of a bicycle has a diameter length 56 cm. Find the covered distance when completing one turn. How many turns should be done to cover a distance of 352 m?



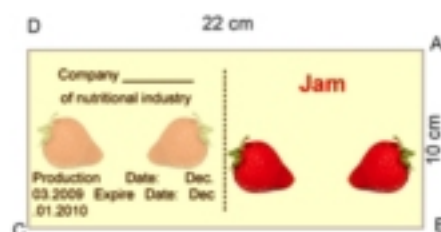
- 4 A jam jar has the form of a cylinder. Its flat base is a circle with diameter length 3.5 cm. Find the circumference of its flat base.



- 5 A piece of paper has the form of a rectangle with dimensions 10 cm and 22 cm is stuck down on the curved surface of the jam jar, where \overline{AB} coincides on \overline{DC} . The height of the jam jar = cm
The circumference of the flat base = cm

Find the radius length of the flat base where ($\pi = \frac{22}{7}$)

- 6 Which figure has greater area; a parallelogram whose base length is 5.4 cm and its corresponding height is 4.1 cm, or a rhombus with diagonal lengths 5.4 cm and 4.1 cm?



Activity

Calculate the perimeter of each of the following figures, where $\pi \approx 3.14$:

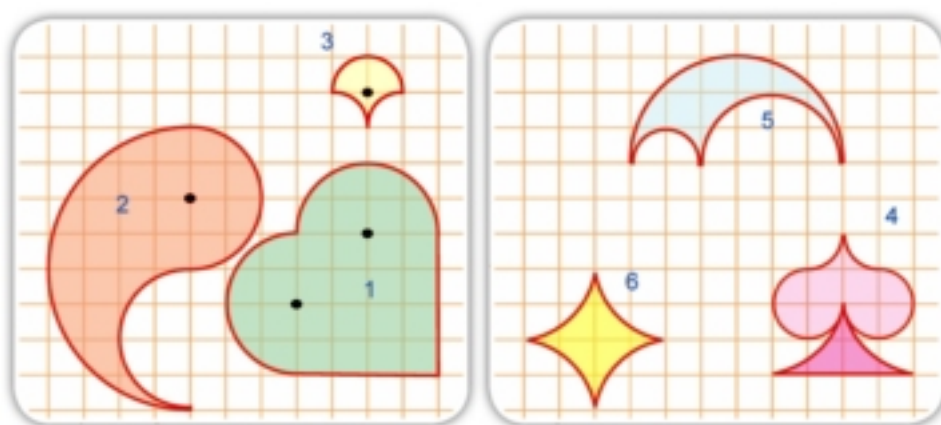
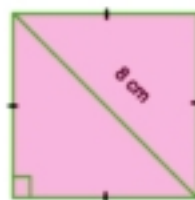
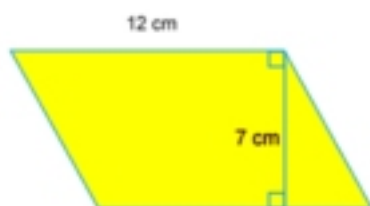
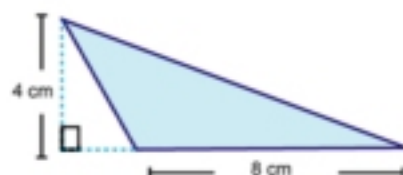
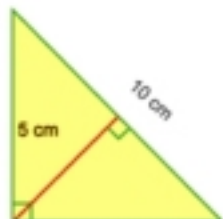


Figure	Perimeter
1
2
3
4
5
6

Test

Unit Test

- 1 Find the area of the following figures :



- 2 If the area of a parallelogram with base length 12 cm and its corresponding height of 6 cm is equal to the area of a rhombus with a diagonal length 10 cm, then find the length of the other diagonal of the rhombus.
- 3 Find the circumference of a circle with diameter length 14 cm ($\pi = \frac{22}{7}$)
- 4 A piece of land has the shape of a parallelogram whose base length is 18 m and its corresponding height 10 m. A flower basin has the shape of a square whose diagonal length is 7 m is placed inside it. Find the area of the surface left .
- 5 If the circumference of a circle is 154 cm, then find its diameter length ($\pi = \frac{22}{7}$)

Unit Four

Geometric transformations

4



Symmetrical figures and axis of symmetry



Think and Discuss

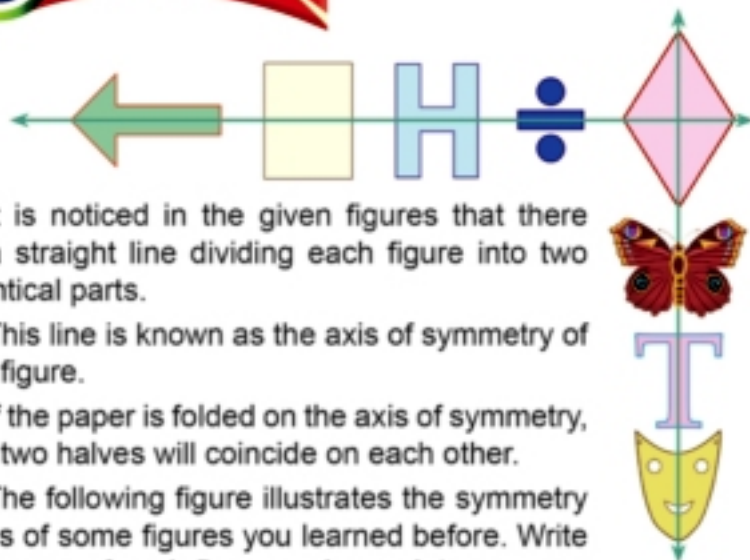
You will learn

- 😊 Symmetrical figures and axis of symmetry.
- 😊 The meaning of reflection.
- 😊 To find the image of a point by reflection across a line.
- 😊 To find the image of a straight segment by reflection across a line.
- 😊 To find the image of a geometric figure by reflection across a straight line.



Key - Terms

- ▶ Geometric transformation
- ▶ Symmetrical figures
- ▶ Reflection
- ▶ Axis of symmetry

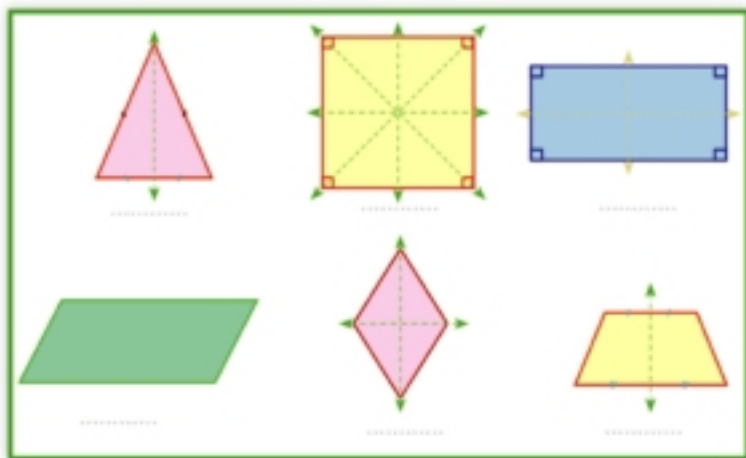


It is noticed in the given figures that there is a straight line dividing each figure into two identical parts.

This line is known as the axis of symmetry of the figure.

If the paper is folded on the axis of symmetry, the two halves will coincide on each other.

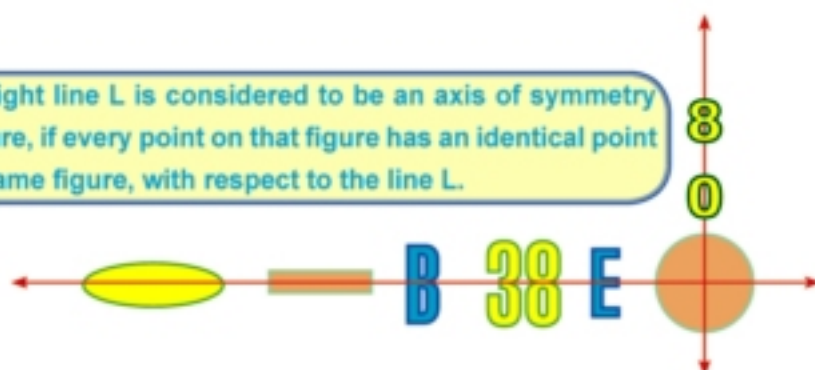
The following figure illustrates the symmetry axes of some figures you learned before. Write the name of each figure and complete:



- A Figures having axes of symmetry are
- B The symmetry axis divides the figure into two halves.
- C The number of symmetry axes of an equilateral triangle =

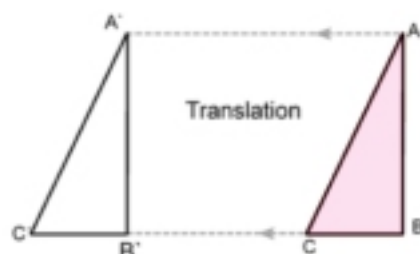
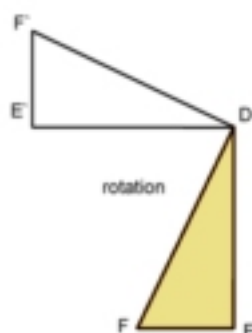
Remark

The straight line L is considered to be an axis of symmetry for a figure, if every point on that figure has an identical point on the same figure, with respect to the line L.

**Geometric transformations**

In the opposite figure, the colored triangle is transformed to another position by reflection, translation or rotation according to a certain system known as geometric transformations.

Each geometric translation has a specific meaning. For example, reflecting the figure which is called **(Reflection)**, moving the figure in a certain direction which is called **(Translation)** and turning the figure around a point with a certain angle which is called **(Rotation)**.

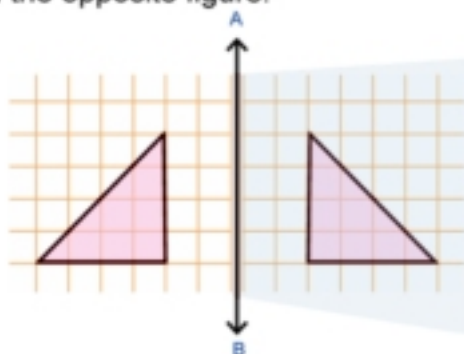
**Remark**

A geometric transformation transforms every point A in the plane to another point A' in the plane itself.

Reflection

Activity

- 1 Draw on a graph paper a triangle as shown in the opposite figure.
- 2 Put a vertical flat mirror on one of the lines like \overleftrightarrow{AB} as shown.
- 3 Observe the reflection of the triangle in the mirror.
 - A Are the lengths of the original triangle straight segments equal to their corresponding images?
 - B Are the straight segments drawn from the vertex of the triangle and their corresponding image perpendicular to the axis \overleftrightarrow{AB} ?



The figure above illustrates a **geometric transformation** called **reflection** and the edge of the mirror represented by \overleftrightarrow{AB} is called the axis of reflection.

Reflection across a line

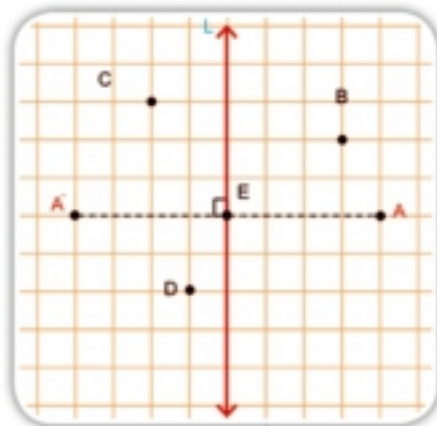
1 The image of a point by reflection:

To find the image of point A by reflection across line L , draw from point A a perpendicular line to L to intersect it at point E and take $A'E = AE$ where $A' \in \overleftrightarrow{AE}$.

Then point A' is the image of point A by reflection across L .

Practice

In the opposite figure: find the image of points B , C and D by reflection across L .



2 The image of a line segment by reflection

To find the image of \overline{AB} by reflection across L :

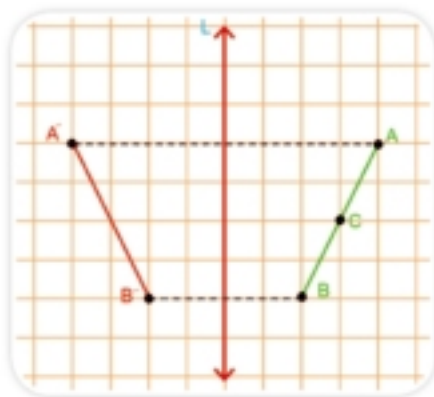
Find the image of point A by reflection across L .

Label it A' .

Find the image of point B by reflection across L .

Label it B' .

Draw $\overline{A'B'}$ to be the image of \overline{AB} by reflection across L .



Practice

In the previous figure:

- ① Given that $C \in \overline{AB}$, Find the image of point C by reflection across L . Label it C' .
Does $C' \in \overline{A'B'}$?

- ② Choose any point $D \in L$, Label it D .

Find the image of point D by reflection across L . Label it D'

Does D' coincide on point D ?

Remark

The image of point A by reflection across line L is A' , and the image of point B by reflection across L is B' where:

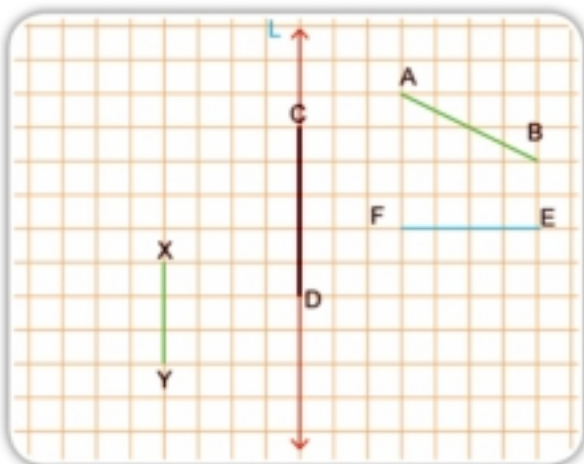
- ① If $A \notin L$ then L bisects the perpendicular segment $\overline{AA'}$.
② If $B \in L$, Then B' coincides on B .



Practice

Find the images of the indicated line segments by reflection across L . Then complete:

- A** The image of \overline{AB} by reflection across L is
- B** The image of \overline{EF} by reflection across L is
- C** The image of \overline{XY} by reflection across L is
- D** The image of \overline{CD} by reflection across L is



Compare the length of each line segment and the length of its image. What do you conclude?



3 The image of a geometric figure by reflection

- 1** Find the image of the triangle ABC by reflection across L :

The triangle ABC is made up of three sides:

\overline{AB} , \overline{BC} and \overline{AC} .

In the opposite figure:

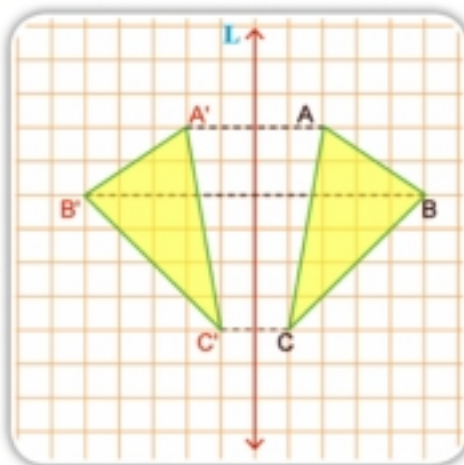
Locate A' the image of A by reflection across L .

Locate B' the image of B by reflection across L .

Locate C' the image of C by reflection across L .

Draw $\overline{A'B'}$, $\overline{B'C'}$ and $\overline{C'A'}$ to get the triangle $A'B'C'$.

$A'B'C'$ the image of triangle ABC by reflection across L .



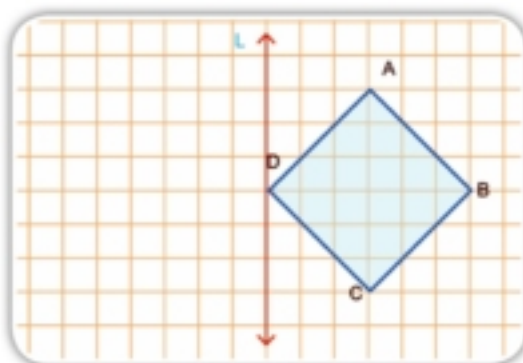
Remark

1	A' is the image of A	i.e.	the image of $\triangle ABC$ by reflection across L is $\triangle A' B' C'$
	B' is the image of B		
	C' is the image of C		

2	The image	is congruent to	preimage	i.e.	$AB = A' B'$,	$m(\angle A) = m(\angle A')$
	$\triangle A' B' C'$	is congruent to	$\triangle ABC$		$BC = B' C'$,	$m(\angle B) = m(\angle B')$
			$CA = C' A'$,		$m(\angle C) = m(\angle C')$	

- 2 Find the image of the square ABCD by reflection across L :

Locate point A' the image of A
 Locate point B' the image of B
 Locate point C' the image of C



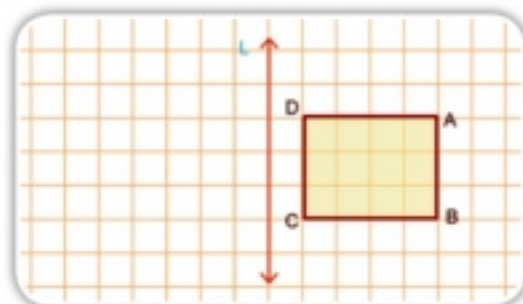
Remark

Point $D \in L$ then D' coincides on the point D itself
 \therefore The image of square ABCD is square $A' B' C' D$.

Practice

- 1 In the opposite figure: Find the image of the rectangle ABCD by reflection across L , then complete:

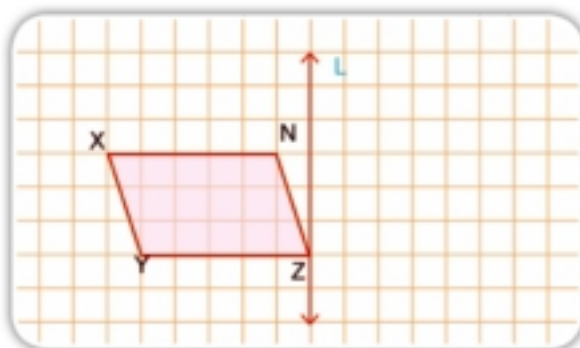
- A The image of the rectangle ABCD by reflection across L is the rectangle
- B $BC = \dots\dots\dots$, and $m(\angle D) = \dots\dots\dots$



- 2** In the opposite figure: Find the image of the parallelogram XYZN by reflection across L, then complete:

A The image of the parallelogram XYZN by reflection across L is the parallelogram...

B $XY = \dots\dots\dots$ and $YZ = \dots\dots\dots$



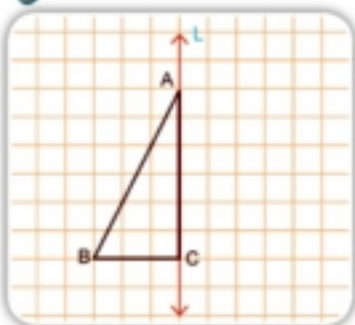
Remark

- 1** To draw the image of a given figure by reflection across line L, the distance between any point of the figure and the axis of symmetry is equal to the distance of its image and the axis of symmetry but on the other side.

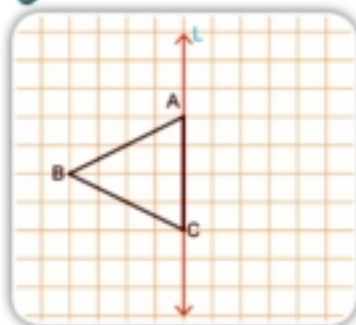
- 2** If point B belongs to axis of symmetry L, then its image coincides on the point itself.

- 3** Determine the image of each figure by reflection across L.

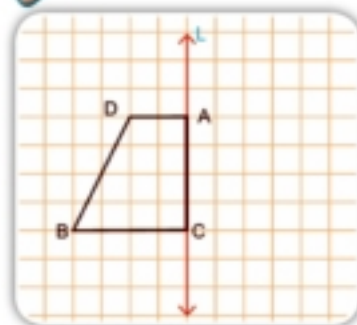
A



B



C

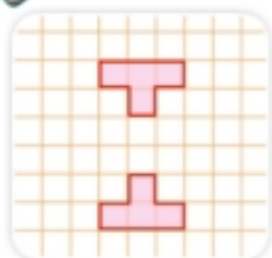


Refer to the previous figures, complete:

- (1) Each figure and its image are
- (2) The image of point A is because it
- (3) The image of point C is because it
- (4) If the paper - where the figure is drawn on - is folded along the axis of symmetry the figure coincides on

- 4 Draw the axis of symmetry to make one of the following figures an image to the other.

A



B

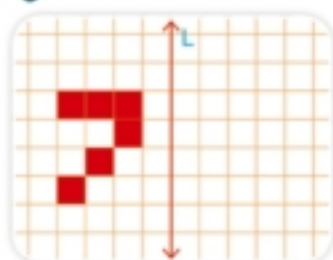


C

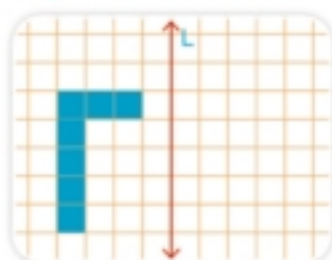


- 5 In the following figures, draw the image of the colored figure by reflection across L.

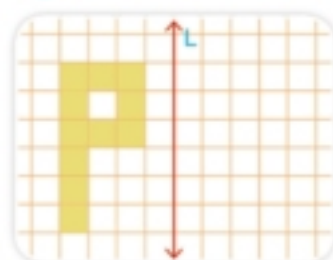
A



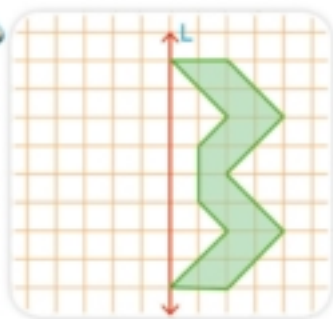
B



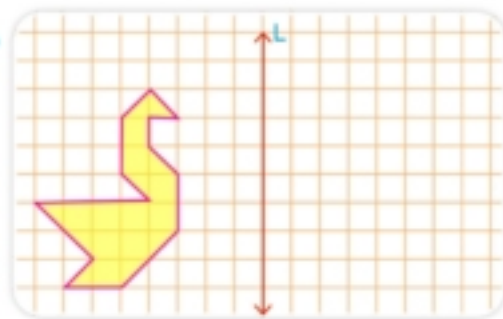
C



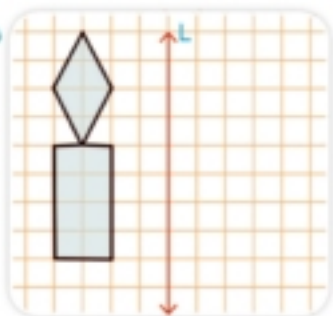
D



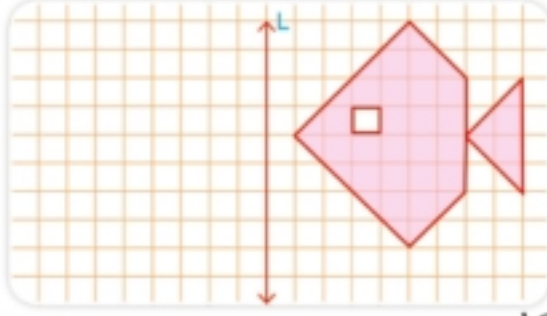
E



F



G



Locating points on a ray



Think and Discuss

* You will learn *

- 😊 To locate points representing numbers on a horizontal ray.
- 😊 To locate points representing numbers on a vertical ray.
- 😊 To locate a point on a coordinate plane.



Key Terms

- ▶ Horizontal ray
- ▶ Vertical ray
- ▶ Coordinate plane

Observe the horizontal ray \overrightarrow{OX} drawn in the following figure:



Start with point O, which represents the number zero, then locate equidistant points to represent the numbers 1, 2, 3, If point A represents the number 4 and point B represents the number 7, then:

The length of $\overline{AB} = 7 - 4 = 3$ units

What is the length of the line segment \overline{OA} ? What is the length of the line segment \overline{OB} ?

Locate point C on the number line to represent the number 9. What is the length of the line segment \overline{AC} and what is the length of the line segment \overline{BC} ?



Practice

On the horizontal ray \overrightarrow{OX} shown in the following figure:



- A** Locate point A to represent the number 1.
- B** Locate point B to represent the number 5.
- C** Locate point C to represent the number 8.
- D** Complete: the length of $\overline{AB} = \dots$ units, the length of $\overline{BC} = \dots$ units and the length of $\overline{AC} = \dots$ units.
- E** Locate point D that bisects the line segment between A and B.

Which number is represented by point D?

When the ray is vertical

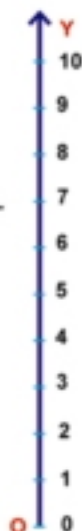


Think and Discuss

In the opposite figure:

The ray \overrightarrow{OY} is a vertical ray and starts with point O which represents the number zero.

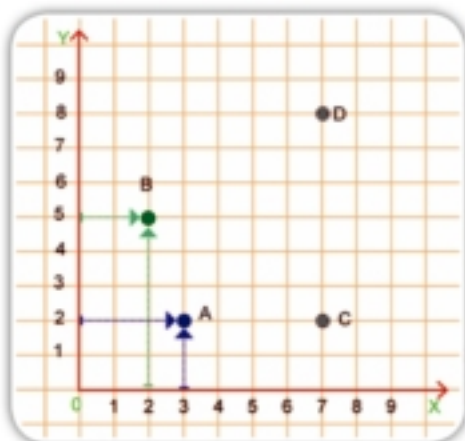
- Locate point A that represents the number 3.
- Locate point B that represents the number 8.
- What is the length of \overline{AB} ?
- If point E is the midpoint of \overline{OB} . What is the length of \overline{OE} ?



Locating points on a coordinate plane

If the horizontal ray \overrightarrow{OX} and the vertical ray \overrightarrow{OY} are drawn, then a **coordinate plane** is constructed as shown in the opposite figure. The location of each point is determined by an **ordered pair**. Each ordered pair determines only one point on the plane.

Where point A (3, 2) and point B (2, 5)



1 Complete:

- A Point C (... , ...) and point D (... , ...)

$AC = 4$ units and $CD = \dots$ units

2 On the figure above, plot the points M (5, 2) and N (5, 8), then complete:

$CM = \dots$ units. $MN = \dots$ units. $ND = \dots$ units.

The name of the figure MNDC is and, the perimeter of the figure MNDC is units.

Exercises

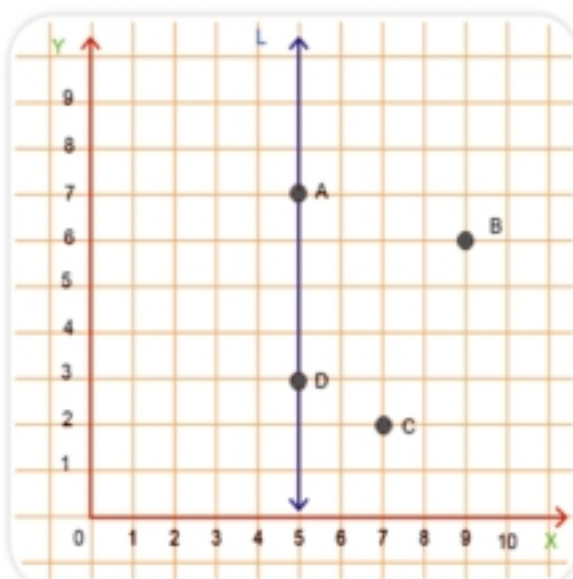
On the coordinate plane illustrated in the opposite figure:

I. Complete: A (....,)

B (....,)

C (....,)

D (....,)



II. If L is the axis of reflection to the figure ABCD, **complete**:

A The image of B by reflection across L is $B'(\dots, \dots)$

B The image of C by reflection across L is $C'(\dots, \dots)$

C The image of A by reflection across L is $A'(\dots, \dots)$

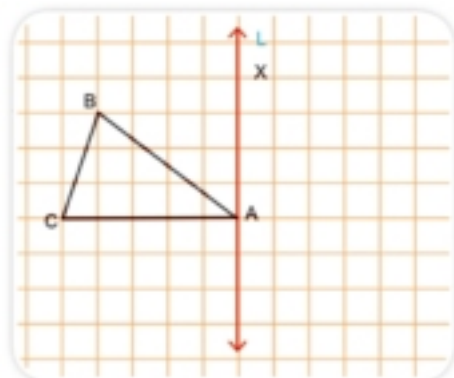
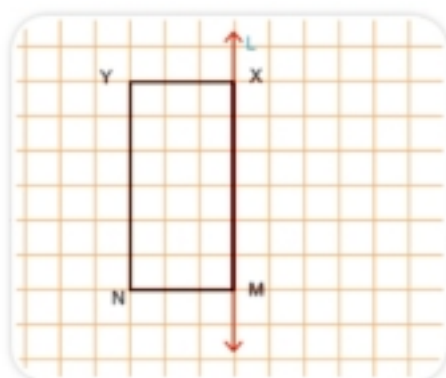
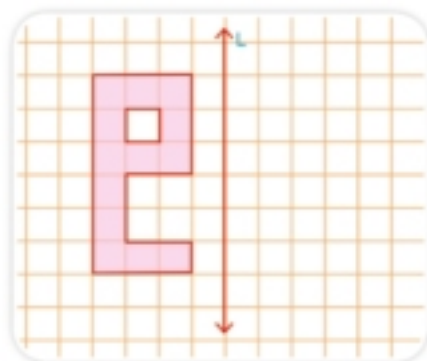
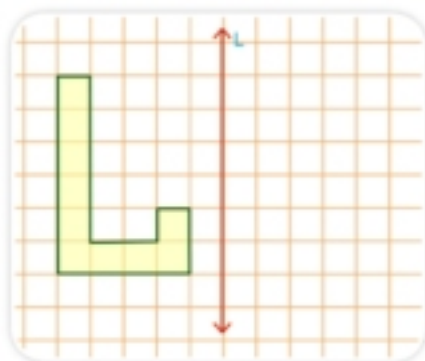
D The image of D by reflection across L is $D'(\dots, \dots)$

III: The image of $\triangle BCD$ by reflection across L is

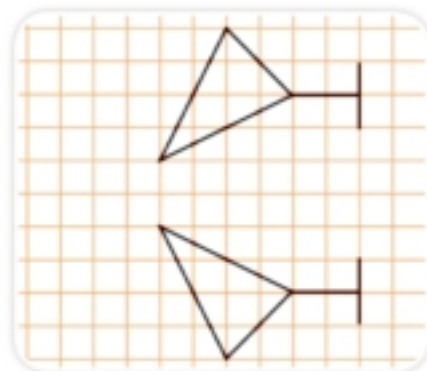
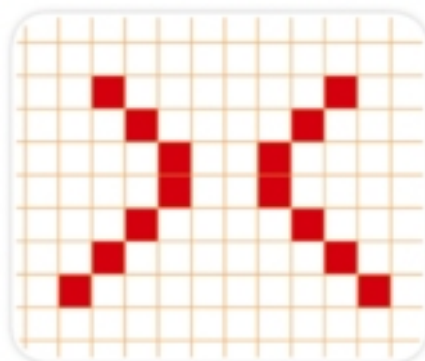
IV: The image of the figure ABCD by reflection across L is

General Exercises

- 1 Find the image of each of the following figures by reflection across L .



- 2 Draw the axis of symmetry to each figure.



- 3 In the opposite figure, \overleftrightarrow{BD} is the axis of reflection.

Complete:

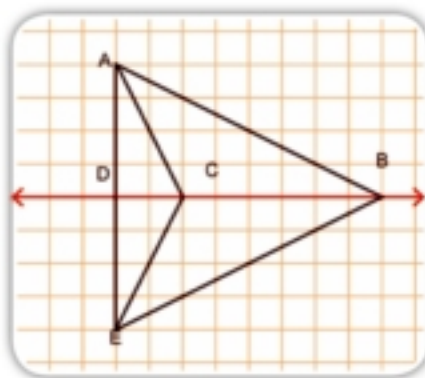
- A The image of $\triangle ABC$ by reflection across \overleftrightarrow{BD} is, then

$AB = \dots$ and $AC = \dots$

- B The image of $\triangle ACD$ by reflection across \overleftrightarrow{BD} is, then

$AD = \dots$ and \overline{CD} coincides on, then

- C $\triangle ABC$ is congruent to $\triangle \dots$ and
 $\triangle ECD$ is congruent to $\triangle \dots$



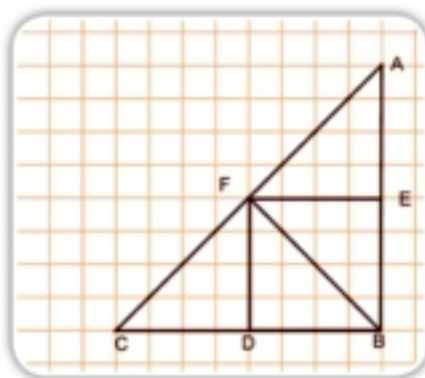
- 4 In the opposite figure: complete:

- A $\triangle BEF$ is the image of $\triangle AEF$ by reflection across

- B $\triangle BDF$ is the image of $\triangle CDF$ by reflection across

- C $\triangle ABF$ is the image of $\triangle CBF$ by reflection across

- D $\triangle BEF$ is the image of $\triangle BDF$ by reflection across

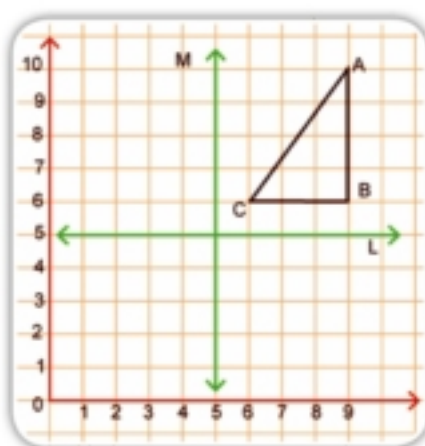


- 5 The opposite figure represents a coordinate plane:

- A Write the coordinates of points A, B, and C.

- B Draw $\triangle A'B'C'$ the image of $\triangle ABC$ by reflection across (L) and determine the coordinates of the vertices A' , B' and C' .

- C Draw $\triangle A''B''C''$, the image of $\triangle ABC$ by reflection across M and determine the coordinates of its vertices A'' , B'' and C'' .



- 6 On the coordinate plane illustrated in the opposite figure:

A Plot the following points.

A (2, 2)

B (5, 2)

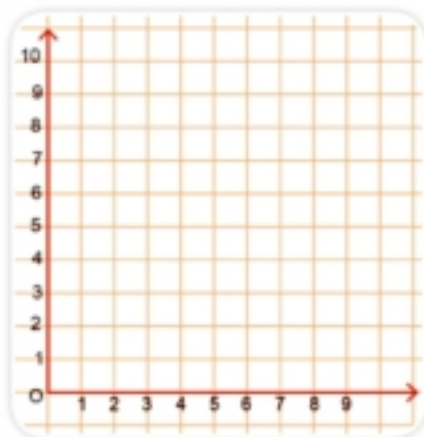
C (5, 8)

D (2, 8)

B Draw the line segments \overline{AB} , \overline{AD} , \overline{CD} and \overline{BC} .

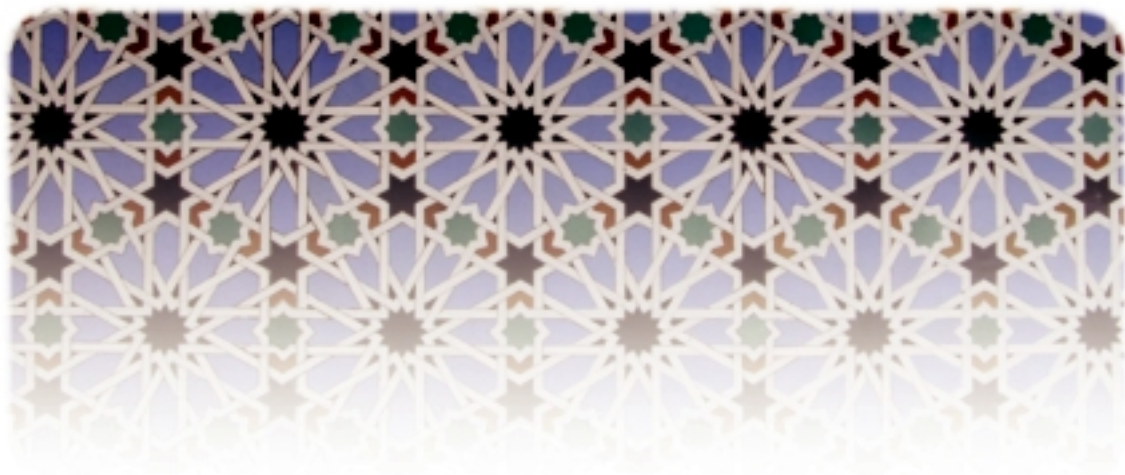
C If \overleftrightarrow{BC} is the axis of reflection of the figure ABCD, then find the image of the figure using the suitable symbols.

D Determine the ordered pairs of the points representing the vertices of the image.



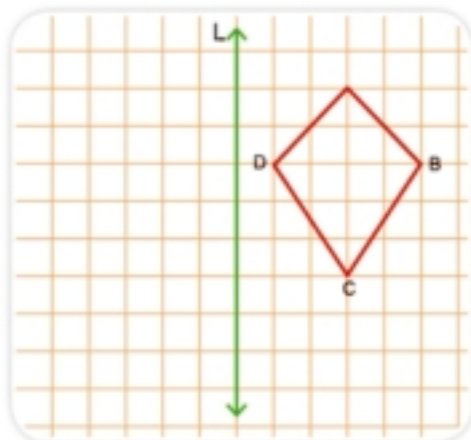
Activity

- 1 Use the coordinate grid net to draw some figures, then locate their images by reflection. Add it to your portfolio.
- 2 Use the reflection to design your own decorative figures.



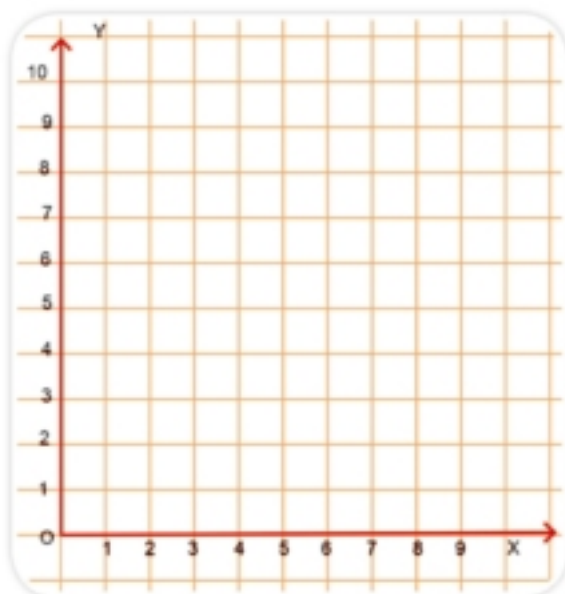
Unit Test

- 1 In the opposite figure: Draw the image of the figure ABCD by reflection across (L).



- 2 On a coordinate plane:

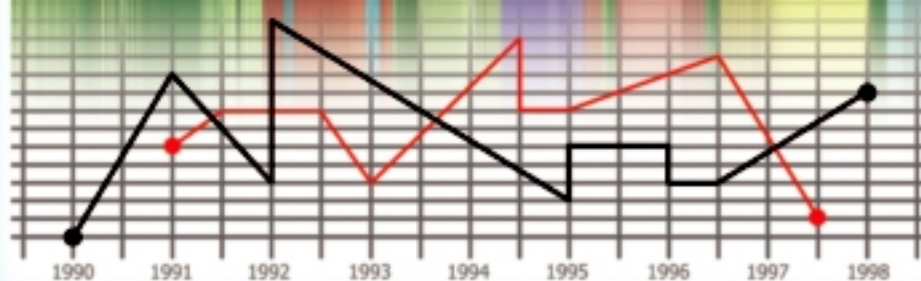
- A Plot the following points :
A (3, 5), B (6, 5) and C (3, 2).
- B Find the length of \overline{AC} .
- C Find the length of \overline{AB} .
- D Draw the image of $\triangle ABC$ by reflection across \overleftrightarrow{AC} and determine the ordered pairs that represent the vertices of the image.



Unit 5

Statistics

5



Collecting data

You will learn

- 😊 To collect data using counting and recording.
- 😊 To collect data using measuring.

Key Terms

- 😊 Collecting data
- 😊 Counting and recording
- 😊 Carrying out a survey of opinion
- 😊 Measuring



Think and discuss

Last friday, Ahmed went with his father to the gas station where his father works. He saw cars refueling and he noticed that some cars were refueling with gasoline 80 while other cars were refueling with gasoline 90 and some were refueling with diesel.



Ahmed asked his father about the difference between each type of gasoline. His father said that gasoline 90 is purer than gasoline 80 and this is suitable for modern cars to preserve the engine while gasoline 80 is used by older cars because it is cheap. However, there is another type of gasoline: gasoline 92 which is the purest of all, but it is not available in that gas station.

As for diesel, it is used by trucks and some other cars equipped to use that type of gasoline.

Ahmed recorded the number of cars and the types of fuel they put in every hour:





Type of fuel	Tallies	Frequencies
	
	
	

Complete the following frequency table, then answer the following questions:

- 1 What is the most wanted type of gasoline at that station?
- 2 What is the least wanted type of gasoline at that station?
- 3 What advice would you give to the manager of that station?



Carry out a survey on your classmates about the sports practiced by them, then answer the following questions

Game	Tallies	Frequencies
Football 
Ping-Pong 
Basketball 
Swimming 

- 1 What is the most popular game for students?
- 2 What is the least popular game for students?
- 3 What advice would you give to your classmates who do not take part in any type of these games?



Use a thermometer and record the temperatures in a week at the following times (8:00 am, 2:00pm, 3:00pm, 6:00 pm and 10:00pm) Arrange the temperatures of every day in an ascending order. Are there any repeated temperatures? on which days? at what time?



Organizing and displaying data



Think and discuss



You will learn

- ☺ To organize and display data using the simple frequency table.
- ☺ To organize and display data using the cumulative frequency table.

Key Terms



- ☺ Simple frequency table
- ☺ Frequency table with intervals

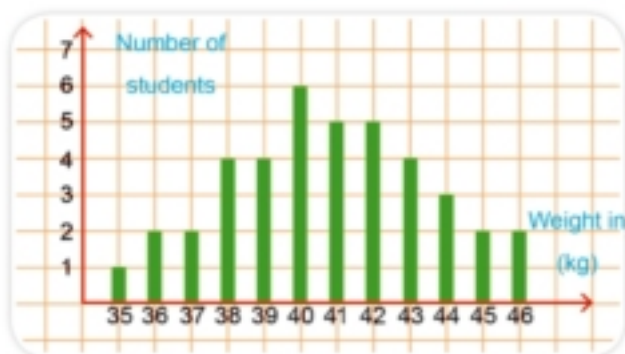
The number of students in my class is 40 students. The senior of the class wanted to record our weights. We brought the scale from the room of the school nurse. Then, we recorded the weights approximated to the nearest kilogram. They were as follows:

41, 37, 40, 42, 44, 41, 45, 38, 42, 43, 37, 38, 42, 46,
39, 45, 40, 36, 40, 38, 42, 42, 41, 40, 43, 39, 40, 41,
39, 41, 43, 40, 39, 38, 35, 46, 44, 36, 44, 43

Our teacher divided us into groups and asked each group to think of a method to organize and display those data.

The first group thought of the following method:

Weight in (kg)	Tallies	Number of students (frequency)
35		1
36		2
37		2
38		4
39		4
40		6
41		5
42		5
43		4
44		3
45		2
46		2

**Note that**

The lightest weight is 35 kgs while the heaviest weight is 46 kgs

The second group thought of the following method:

Weights	Tallies	Frequencies
35, 36		3
37, 38		6
39, 40		10
41, 42		10
43, 44		7
45, 46		4

The third group thought of the following method:

Weights	Tallies	Frequency
35, 36, 37		5
38, 39, 40		14
41, 42, 43		14
44, 45, 46		7

it can be written also

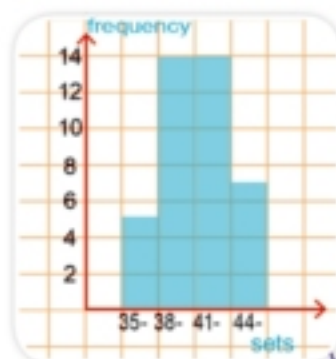
in the form →

where (35-) means that weight is ranging from 35 kgs to less than 38 kgs.

Sets	Frequency
35-	
38-	
41-	
44-	



In your opinion, which method of the three is the easiest?
Why?



Exercises

- 1 The following are the marks of 32 students in the final math exam for the first term:

25	30	38	41	47	48	50	32
37	46	48	26	38	40	42	30
35	50	40	37	39	48	49	47
36	45	35	42	41	40	36	44

First: complete: the lowest mark is

the highest mark is

Second: Think of a method to display those marks in suitable sets.

Form the cumulative frequency table with sets for these data. Can you display those data in another way? Explain your answer.

- 2 The teacher asked the students to head for the student's affairs official in order to determine the days of absence for each student in the class. The number of students was 40 students and the data were as follows:

2	1	5	0	3	1	4	1	2	6
0	2	1	3	5	4	1	2	1	0
3	1	0	4	4	2	1	0	1	3
1	2	6	7	1	4	3	4	2	3

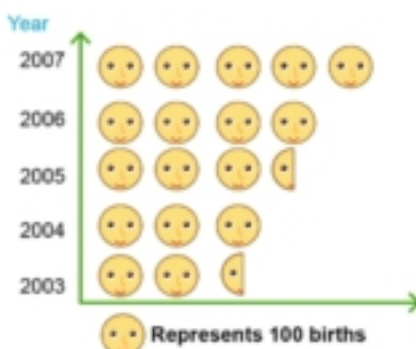
Form the frequency table that represents these data, then represent them by a bar graph.

Reading tables and line graphs



Think and discuss

The opposite data representation shows the number of babies who were born at a hospital from 2003 to 2007. From the drawing, find:



First: The number of births at that hospital in 2005.

Second: The increase in the number of births in 2007 compared to 2003.

Solution

First: The number of births in 2005

$$= 100 \times 3 + 50 = 350 \text{ births}$$

Second: The number of births in 2007

$$= 100 \times 5 = 500 \text{ births.}$$

The number of births in 2003

$$= 100 \times 2 + 50 = 250 \text{ births.}$$

The increase of births in 2007 Compared to 2003 =

$$500 - 250 = 250 \text{ births.}$$



What is the increase in births at that hospital in 2006 compared to 2004?

You will learn

- ☺ To represent data using pictures (pictographs).
- ☺ To represent data using bar graphs.
- ☺ To represent data using double bar graphs.

Key Terms

- ☺ Representing data by pictures (pictographs)
- ☺ Representing data by bar graphs
- ☺ Representing data by double bar graphs

Think and discuss

The opposite bar graph shows what Samir, Adel, and Mohamed have saved during the first five months of the year. Complete:

- A** The savings of Samir are equal to the savings of Adel in April and in
- B** The savings of Mohamd are equal to the savings of Adel in
- C** The savings of Samir are greater than the savings of Adel in and

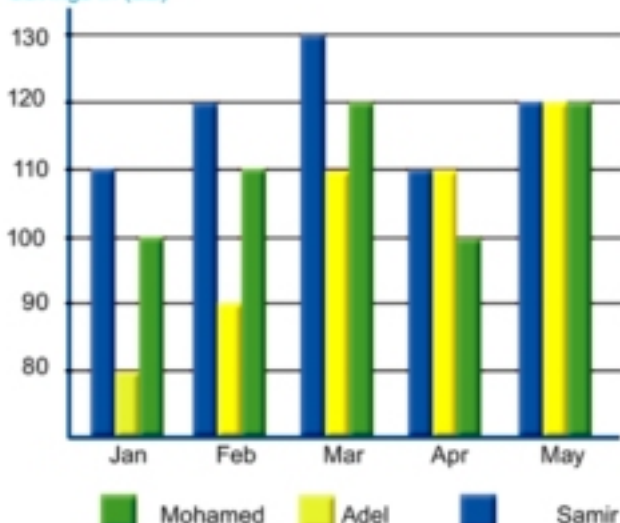
Practice

The following figure shows the sales of TVs, computers, and air conditioners in thousands of pounds in a store during five successive days:

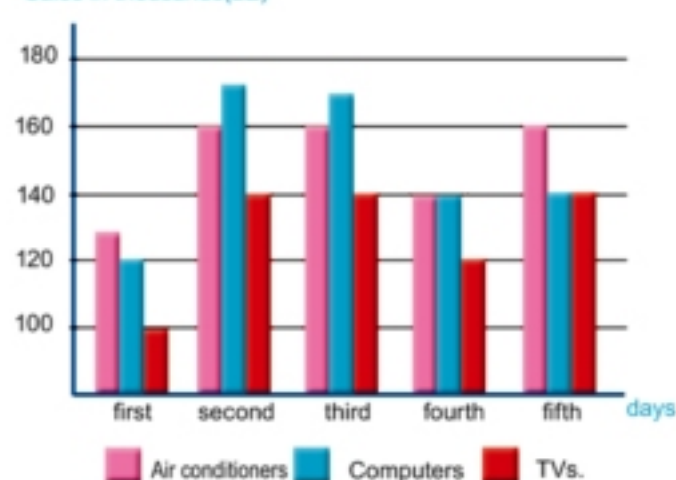
Complete:

- A** The day in which the sales of air conditioners are equal to the sales of computers is
- B** The day in which the sales of the TVs are equal to the sales of computers is
- C** The days in which the sales of computers are greater than the sales of televisions are and
- D** The days in which the sales of TVs are smaller than the sales of air conditioners are

Savings in (LE)



Sales in thousands(LE)



Representing data by the histogram and the frequency polygon

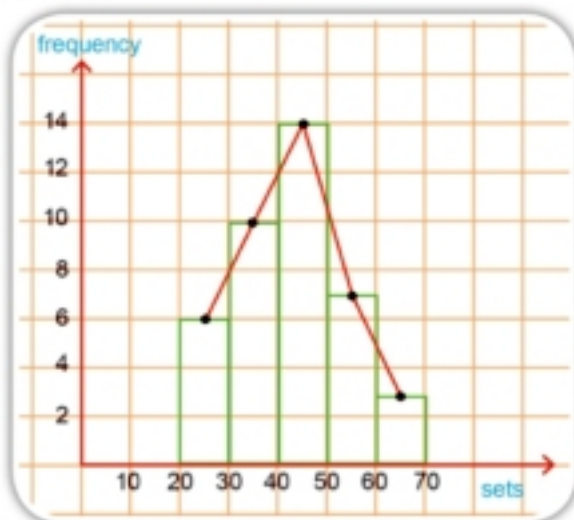


Think and discuss

Magdy and Yasser visited a company to collect some data about the daily wages paid for workers. They recorded the data and formed the following cumulative frequency table with sets.

Sets	20-	30-	40-	50-	60-	Total
Frequency	6	10	14	7	3	40

Their teacher asked them to represent the data using the frequency polygon.



Magdy said:

First, I can draw the histogram that I learned, then:

- 1 I bisect the upper bases of the rectangles that form the histogram.
- 2 I draw line segments that join the points of bisection in order.
- 3 The union of the line segments is called the frequency polygon. In the above figure, it is colored in red.

You will learn

- ☺ To represent data using the frequency polygon.

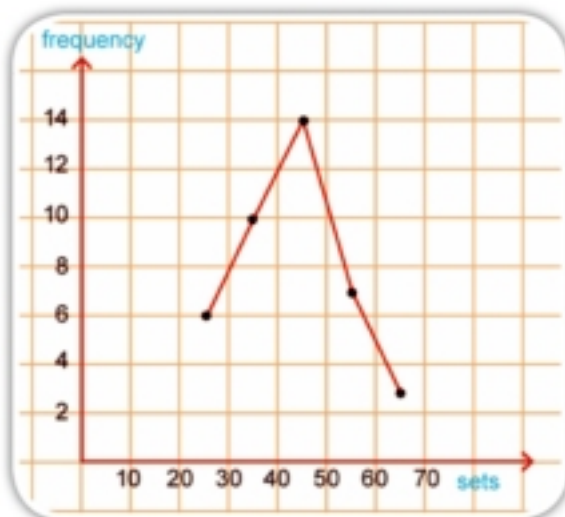
Key Terms

- ☺ The frequency polygon

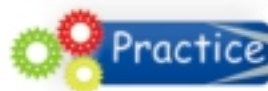
Yasser said:

I would follow another method to draw a frequency polygon as follows:

- 1 I would draw the two axes (the horizontal and the vertical), then I would divide each of them into equal parts to distribute the given data.
- 2 I would determine the center of each set. For example, the set 20- its center is $\frac{30 + 20}{2} = 25$, The set 30 - its center is 35 and so on.....
- 3 I would determine the points which represent the ordered pairs (the center of the set, the frequency).
- 4 I would draw line segments that join these points in order, thus I would finish drawing the frequency polygon.



Which method would you prefer: Magdy's or Yasser's method? and why?



The following table represents the marks of 50 students in the math exam in a month, where the full mark is 50.

Sets	10 -	20 -	30 -	40 -	Total
Frequency	10	12	18	10	50

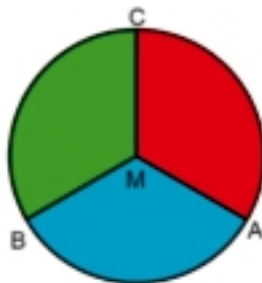
Draw the frequency polygon which represents the given data.

Representing data using the pie graphs



Think and discuss

In the following figure; A circle whose center is M has the radii \overline{MA} , \overline{MB} and \overline{MC} . Those radii divide the surface of the circle into 3 equal sectors, each of them is called a **pie graph**.



You will learn

To represent data using pie graphs.



Practice

Complete:



The colored sector represents of the circle



The colored sector represents of the circle



The colored sector represents of the circle

Example

Ahmed, Hossam and Hanan have bought Pizza for dinner and paid LE 24. Ahmed paid LE 12, Hossam paid LE 8, and Hanan paid the rest. The pizza has been divided into sectors according to the amount of money each paid. Graph the given data.

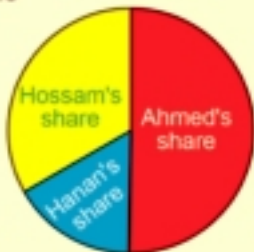
Solution

Hanan paid = $24 - (12 + 8) = \text{L.E } 4$

Ahmed's share = $\frac{12}{24}$ of the pizza = $\frac{1}{2}$ of the pizza.

Hossam's share = $\frac{8}{24}$ of the pizza = $\frac{1}{3}$ of the pizza.

Hanan's share = $\frac{4}{24}$ of the pizza = $\frac{1}{6}$ of the pizza.



Key Terms

Pie graph

Exercises

- 1 The following table shows the recorded temperatures in 40 cities on a day.

Temperatures	20 -	22 -	24 -	26 -	28 -	Total
Number of cities	7	9	11	8	5	40

Required:

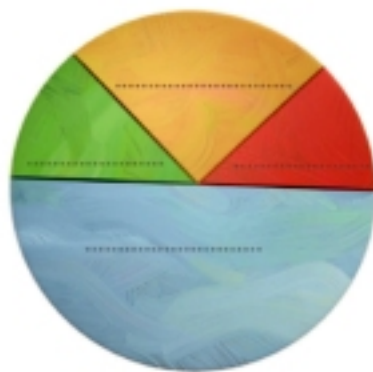
- A The number of cities with temperatures less than 24 degrees Celsius.
 B Draw each of the histogram and the frequency polygon.
- 3 The following frequency distribution shows the marks of a group of students in an exam.

Sets	5 -	10 -	15 -	20 -	25 -	30 -	35 -	Total
Number of students	3	6	8	12	10	6	5	50

First: What is the number of students who got 30 marks or more.

Second: Draw the frequency polygon for that distribution.

- 3 An employee spends his salary as follows:
 LE 200 for clothes.
 LE 800 for food.
 LE 400 for transportation and medicine.
 LE 200 for renting an apartment.
 Graph that data on the opposite circle.



- 4 A librarian made an inventory of the books in his library and their types. He found the following: $\frac{1}{4}$ of the books are religious, $\frac{1}{4}$ of the books are literary, $\frac{1}{2}$ of the books are scientific.
 Graph that given data using a pie graph. If the total of books was 800, find the number of each type of books.



Activity

Activity

When some students were asked about the most popular TV programs, the following data were extracted:

- $\frac{1}{2}$ of the students like to watch sports programs.
- $\frac{1}{4}$ of the students like to watch cultural programs.
- $\frac{1}{8}$ of the students like to watch Arabic and foreign movies.
- $\frac{1}{8}$ of the students like to watch news.

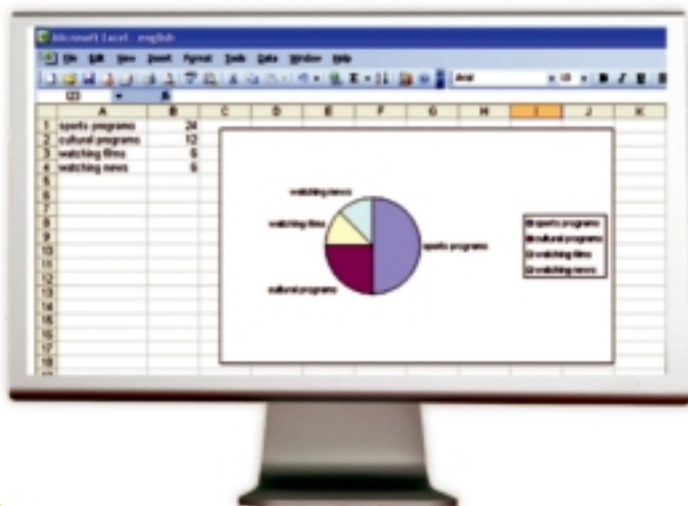
A Represent that given data using a pie graph.

B If the number of students in the class was 48 students, what is the number of students who prefer watching each type of programs?

Technology

Using technology to solve the portfolio

- 1 Open the excel program.
- 2 Record data in the column A (types of programs) in the column B (number of students).
- 3 Shade the data in A and B by the mouse.
- 4 From the insert bar, do a mouse click on chart then pie after that next and next and finish. You will have the required pie graph.



Use the Excel program to solve problem No(4) on page (96)

Test

Unit test

- 1 The following table shows the frequency of the marks of some students in Mathematics.

Sets	5 -	10 -	15 -	20 -	25 -
Frequency	III	III III	III III III	III II	II

First: Rewrite the previous frequency table representing the frequencies by numbers.

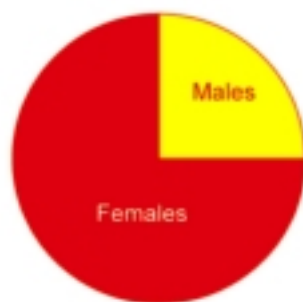
Second: What is the number of students who got marks less than 15.

Third: Draw the frequency polygon for that distribution.

- 2 Draw the frequency polygon for the following frequency distribution:

Sets	10 -	12 -	14 -	16 -	18 -	20 -	Total
Frequency	2	5	7	11	6	4	35

- 3 220 candidates have applied for a test to hire male and female anchor persons in the television. If the opposite pie graph represents the given data; what is the number of female candidates who applied for that test?

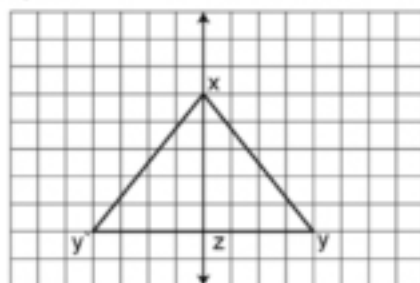


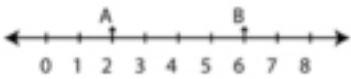
Test (I)

Test

First: choose the correct answer:

1. $7 - 5$ ☐ N. (C, \neq , \notin , \in)
2. The set of even numbers (E) \cap The set of prime numbers (P) = (P, N, O, {2})
3. If we add 3 to the twice of number X, we get (3x, 3+x, 2x+3, 2x)
4. $(93+7) - (7+93) =$ (0, 10, 100, 1000)
5. The perimeter of an equilateral triangle whose side length L cm =cm (L+3, 3L, 6+L, 6L)
6. The area of a triangle equals 20 cm^2 , one of its heights is 5 cm, the length of the correspond base iscm (4, 8, 16, 64)
7. The circumference of a circle of radius 4cm = $\pi \times$ cm (4, 8, 16, 10)
8. In the opposite figure : Δxyz transforms in to $\Delta x'y'z'$ then this transformation is called (Reflection, Translation, Rotation, Otherwise)

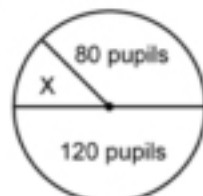


9. $(4 \times 31) \times 25 = (31 \times \dots) \times 25$ (2, 4, 3, 5)
10. The area of a rhombus whose diagonals lengths are 12cm, 16cm = cm^2 (56, 69, 96, 192)
11. On the number line :  the length of $\overline{AB} =$ unit length (2, 4, 5, 6)

Test

- 12 The area of a square of diagonal length 10 cm =cm²
(25 , 50 , 100 , 400)

- 13 In the opposite circular sector :
X representspupils
(40 , 80 , 120 , 240)



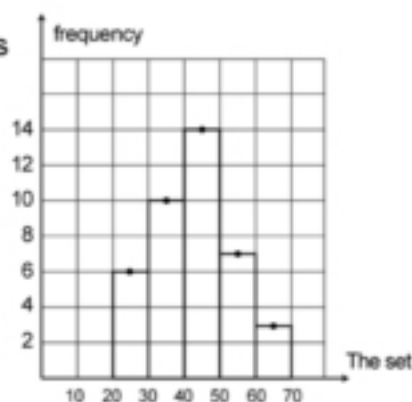
- 14 The opposite table shows the marks of 40 pupils in one test

The Sets	10–	20–	30–	The sum
frequency	10	12	18	40

- the number of pupils who got 30 marks and more =
(18 , 44 , 40 , 80)

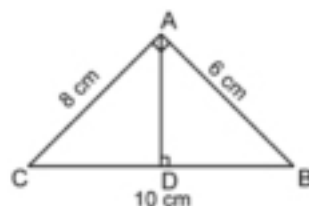
Second: Complete

- 15 13 , 16 , 19 , , (in the same pattern)
- 16 The symbolic expression of multiplying 5 by the number x is
- 17 The natural numbers less than 2 are
- 18 The area of a square whose diagonal 6 cm =cm²
- 19 If the point A lies on the axis of reflection , then its image by reflection in L
- 20 The radius of a circle which circumference 88cm = cm
- 21 The opposite figure shows the marks of 40 pupils
in one test . the number of pupils who got less
than 40 mark =
- 22 The solution set of the equation $X - 2 = 2$
in N is

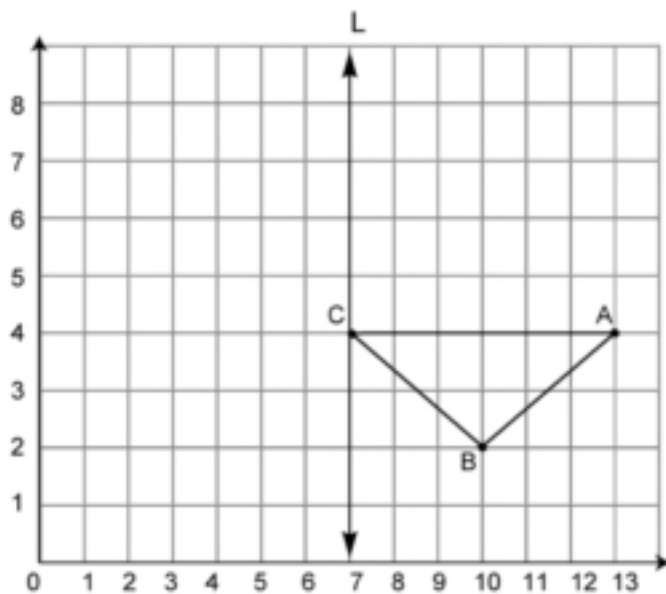


Third: Find the result of :

- 23 Two numbers , their sum equals 35 , one of them is x , what is the other number.
- 24 Using the properties of addition operation in N , find the result of $(53 + 67 + 47)$
- 25 In the opposite figure ABC is right - angled triangle at A , $\overline{AD} \perp \overline{BC}$, Find the length of \overline{AD}



- 26 On the coordinate plane , if L is the axis of reflection for the triangle ABC , draw the image of $\triangle ABC$ in the straight line L .



Test

Test (2)

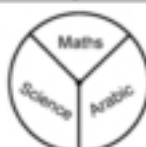
First: choose the correct answer:

- 1 The symbolic expression for the double of the number y is
($y+2$, $2y$, y , $y-2$)
- 2 The set of even numbers (E) \cap the set of odd numbers (O)=.....
(0 , 2 , 1 , \emptyset)
- 3 A Circle of diameter 28cm , its circumference =
(22 , 44 , 88 , 56)
- 4 The smallest natural number is (0 , 1 , 2 , 10)
- 5 If $86 \times 15 = 86 \times X + 86 \times 10$, then $X =$ (10 , 5 , 15 , 20)
- 6 $(8 \div 4)$ N (\in , \notin , \subset , \supset)
- 7 The area of the square of diagonal length 8 cm =.....cm²
(16 , 32 , 64 , 96)
- 8 The area of the rhombus of diagonals lengths 6 cm , 8cm =.....cm²
(12 , 24 , 48 , 96)
- 9 The circular sector which represents the following data number

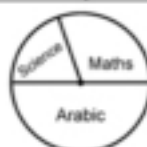
The Subjst	Arabic	Maths	Science
Number of studying hours	3	2	1



(1)



(2)

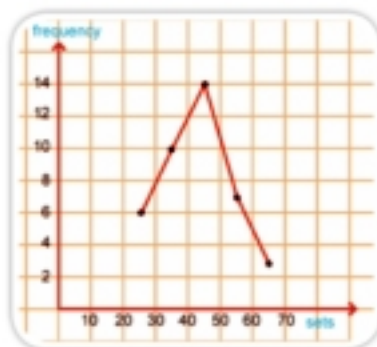


(3)

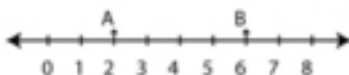


(4)

- 10 The frequency polygon represents the marks of 40 pupils in one test, the centre of the set 40- is
(14 , 40 , 45 , 50)
- 11 The area of a triangle of base length 12cm , its corresponding height 5cm =cm²
(30 , 60 , 17 , 34)



- 12 In the opposite figure:



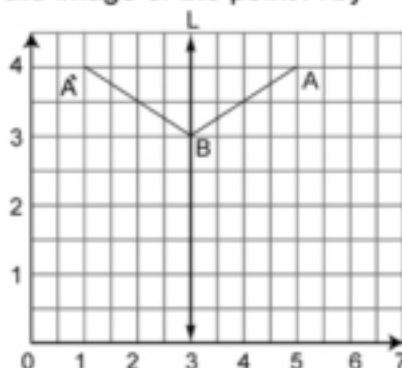
the length of \overline{AB} = unit length (1 , 4 , 6 , 7)

- 13 The area of a square whose perimeter 32cm =cm²

(128 , 32 , 64 , 1024)

- 14 On the coordinate plane in the opposite figure the image of the point A by reflection in L is

[(5,4) , (3,3) , (1,4) , (4,1)]



Second: Complete

- 15 If x is an odd number , then (X+1) is number

- 16 In the opposite figure



M , N are two natural numbers , then <

- 17 If we add 3 to a number X , the result will be

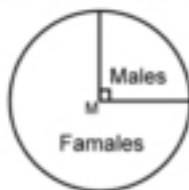
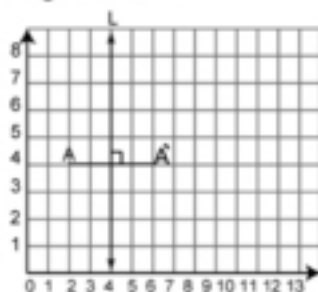
- 18 The area of the rhombus in which the length of its side is 10cm and corresponding height is 9.6cm =cm²

- 19 The straight line L is calledfor the line segment $\overline{AA'}$

- 20 $213 + 57 = 57 + \dots$

- 21 If $2X = 4$,then $4X = \dots$

- 22 200 candidates have applied for a test to hire male and female anchor persons in the television.If the opposite pie graph represents the given data the number of female candidates who applied for that test is



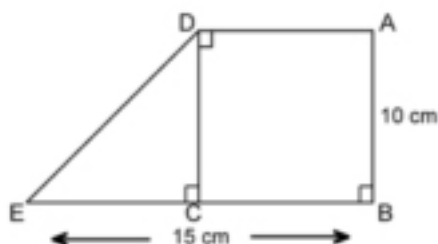
Test

Third: Find the result of :

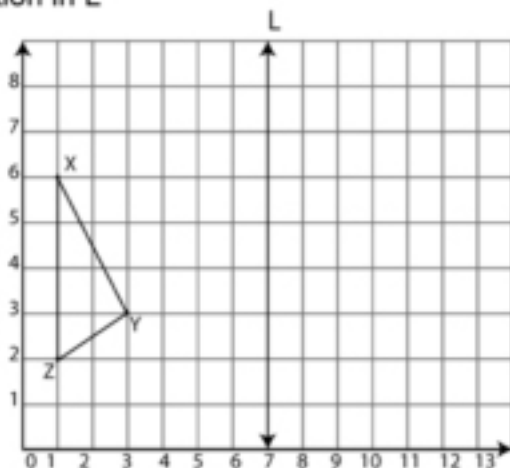
23 Use the distributive property to
Find : $45(10 + 2)$

24 Find the solution set of : $X - 7 = 33$, $X \in \mathbb{N}$

25 In the opposite figure :- ABCD is a square of side length 10cm ,
 $E \in \overline{BC}$, $BE = 15\text{cm}$
Find the area of the shape ABED .



26 In the coordinate plane , if L is the axis of reflection of the shape XYZL,
draw its image by reflection in L




Test (3)

Test

For the special needs

First: choose the correct answer:

- 1 The smallest natural number is (0 , 1 , 2)
- 2 If $7 \times 15 = X \times 15$, then $X =$ (7 , 8 , 9)
- 3 If we multiply the number (X) by 5, then we shall get the number
(X+5 , 5X , X-5)
- 4 The set which represents the set of points  on the number line is the set =
(odd , even , prime)
- 5 If E is the set of even numbers , then E N (\subset , \in , \notin , $\not\subset$)
- 6 The following table is shows the recorded temperatures in 40 cities on a day

Temperatures	20 –	22–	24 –	26 –	28 –	Total
Number of cities	7	9	11	8	5	40

The number of cities with temperatures less than 24 degree celsiuscity
(11 , 16 , 27)
- 7 5075 ☐ 5705 (> , < , =)
- 8 The area of the square which its diagonal length 6cm =cm²
(12 , 18 , 81)
- 9 The solution set of the equation $X-5 = 19$ ({14} , {24} , {5})
- 10 The circumference of a circle of radius 35cm is.....cm ($\pi = \frac{22}{7}$)
(110 , 202 , 220)

Second: Complete each of the following by using the answers between the brackts.
(24 , 4 X , C , D , commutative)

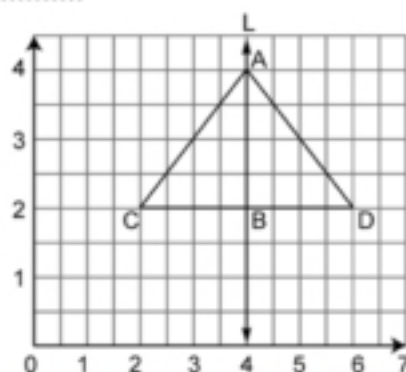
- 1 A rhombus of diagonal lengths 6cm , 8cm ,its area =cm²
- 2 The perimeter of a square of side length Xcm =cm

Test

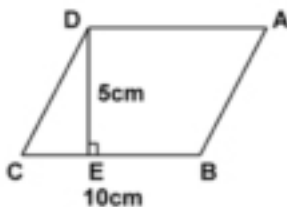
- 3 On the coordinate plane in the opposite figure the image of the point C by reflection in the straight line L is

- 4 $327 \times 8 = 8 \times 327$
(..... property)

- 5 The set of natural numbers $(N) \cap$ The set of counting numbers $C =$



Third: Join from the column (A) to the suitable from the column (B) :

(A)	(B)
(1) If $X+3 = 8$, then $X =$	\in
(2) $(24 \div 6)$N	the length of the diagonal
(3) The circumference of a circle $= \pi \times$	5
(4) The area of the opposite parallelogram =cm ²	50
	32
(5) 8 , 16 , 24 , (in the same pattern)	

المواصفات الفنية:

١٥٢٢/١٠/١٥/٢٢/٥/٢٧	رقم الكتاب:
$\frac{1}{8}$ (٨٢ × ٥٧) سم	مقاس الكتاب:
٤ ألوان	طبع المتن:
٤ ألوان	طبع الغلاف:
٨٠ جم أبيض	ورق المتن:
٢٠٠ جم كوشيه	ورق الغلاف:
١١٢ صفحة	عدد الصفحات بالغلاف:

<http://elearning.moe.gov.eg>

الأشرف برنتنج هاوس